

UNIT-3

Understand the Number Systems

Number systems:

Number system contains a set of numbers that have common characteristics. In any number system; three aspects determine the value of each digit with in a number.

- ✓ The digit itself.
- ✓ The position of the digit in that number
- ✓ The base of the number system

3.1 various number systems used in digital computer:

The most important number systems for computer are:

- Decimal number system
- Binary number system
- Octal number system
- Hexadecimal number system

Radix(or) Base of a number:

The base of a number system is the number of different symbols or digits used in that system.

1)Decimal number system:

- ✓ The number system that we use in our day-to-day life is called the decimal number system.
- ✓ It is positional number system and is the mostly widely used system for representing numbers.
- ✓ In decimal number system the BASE is 10,because it uses 10 different symbols or digits(i.e.) 0,1,2,3,4,5,6,7,8,9 (0 to 9).

Example: The decimal number 1234(written as $(1234)_{10}$) represents the Polynomial.

POSITION	3	2	1	0
VALUE(WEIGHTS)	10^3	10^2	10^1	10^0
DECIMAL POINT	1	2	3	4

$$=(1 \times 10^3) + (2 \times 10^2) + (3 \times 10^1) + (4 \times 10^0)$$

$$=(1 \times 1000) + (2 \times 100) + (3 \times 10) + (4 \times 1)$$

$$=1000 + 200 + 30 + 4$$

$$=1234$$

$$=(1234)_{10}$$

2) Binary number system:

- ✓ Binary number system is a very important number system so far as the digital computers concerned, because computers work with binary numbers.
- ✓ Binary number system is the positional binary system.
- ✓ The BASE of Binary number system is 2 and it uses two digits (i.e.) 0 & 1.
- ✓ These symbols or digits are abbreviated as bits. Thus the word bit stands for either of the binary digits namely 0 or 1.

Example: the decimal equivalent of the binary number 11010 is

POSITION	4	3	2	1	0
VALUE(WEIGHTS)	2^4	2^3	2^2	2^1	2^0
BINARY POINT	1	1	0	1	0

$$(11010)_2 = (1 \times 2^4) + (1 \times 2^3) + (0 \times 2^2) + (1 \times 2^1) + (0 \times 2^0)$$

$$= (1 \times 16) + (1 \times 8) + (0 \times 4) + (1 \times 2) + (0 \times 1)$$

$$= 16 + 8 + 0 + 2 + 0$$

$$= 26$$

$$(11010)_2 = (26)_{10}$$

3) Octal number system:

- ✓ The base or radix of the octal number system is 8, because it uses 8 symbols or digits (i.e.) 0,1,2,3,4,5,6,7
- ✓ This system is also used in computer industry.
- ✓ This system was issued to provide a shorthand way to deal with long strings of 0's & 1's creates in binary.

Example: the decimal equivalent of the octal number 2056 is

POSITION	3	2	1	0
VALUE(WEIGHTS)	8^3	8^2	8^1	8^0
OCTAL POINT	2	0	5	6

$$(2056)_8 = (2 \times 8^3) + (0 \times 8^2) + (5 \times 8^1) + (6 \times 8^0)$$

$$= 2 \times 512 + 0 \times 64 + 5 \times 8 + 6 \times 1$$

$$= 1024 + 0 + 40 + 6 = 1070$$

$$(2056)_8 = (1070)_{10}$$

4) Hexadecimal Number System:

- ✓ The base or radix of the octal number system is 16, because it uses 16 symbols or digits
- ✓ The first ten symbols are represented by digits 0 to 9 and the remaining six by the letters 'A' through 'F'.

A=10, B=11, C=12, D=13, E=14, F=15.

- ✓ This number system is also used to provide a shorthand way to deal with long strings of 0's and 1's created in binary.

Example: Decimal equivalent of Hexadecimal number AF3D is

POSITION	3	2	1	0
VALUE(WEIGHTS)	16^3	16^2	16^1	16^0
HEXA-DECIMAL POINT	A	F	3	D

$$\begin{aligned} (AF3D)_{16} &= (A \times 16^3) + (F \times 16^2) + (3 \times 16^1) + (D \times 16^0) \\ &= (10 \times 4096) + (15 \times 256) + (3 \times 16) + (13 \times 1) \\ &= 40960 + 3840 + 48 + 13 \\ &= 44861 \\ (AF3D)_{16} &= (44861)_{10} \end{aligned}$$

Comparison of the Binary, Octal, Decimal and Hexadecimal:

Attribute	Binary	Octal	Decimal	Hexadecimal
Base	2	8	10	16
Lower Digit	0	0	0	0
Highest Digit	1	7	9	F

IMPORTANT TABLE EQUIVALENT VALUES OF DIFFERENT SYSTEM:

Decimal System	Binary System	Octal System	Hexadecimal System
0	0000	0	0
1	0001	1	1
2	0010	2	2
3	0011	3	3
4	0100	4	4
5	0101	5	5
6	0110	6	6
7	0111	7	7
8	1000	10	8
9	1001	11	9
10	1010	12	A
11	1011	13	B
12	1100	14	C
13	1101	15	D
14	1110	16	E
15	1111	17	F
16	10000	20	10

3.2 Convert Decimal Number into Binary Number:

- The integer and fractional parts of the decimal number are dealt with separately.
- Divide the integer part of the given decimal number repeated by 2 and writing down the remainder after each division.
- The remainder are then taken in reverse order (bottom to top) to form the binary equivalent of the integer part of the decimal number.
- The Fractional part of the given decimal number is multiplied repeatedly by 2 each time recording carry.
- The integers (carry) taken from (top to bottom) to form the binary equivalent of fractional part to the decimal number.

EXAMPLES on Conversion of Decimal Number into Binary Number:

Example 1:

Convert decimal number 125 into binary number

Answer:

It is integer part then Divide the given decimal number repeated by 2 and writing down the remainder after each division.

Division	Remainder
2 125	
2 62	→ 1
2 31	→ 0
2 15	→ 1
2 7	→ 1
2 3	→ 1
2 1	→ 1
0	→ 1

It is an integer part the remainder is taken from bottom to top is 1111101 Thus $(125)_{10} = (1111101)_2$

Example 2:

Convert decimal number 0.4375 into binary number

Answer:

It is a Fractional part then multiplies the given decimal number repeatedly by 2 each time recording carry.

Multiplication	product	carry
0.4375×2	$= 0.8750$	----- 0
0.8750×2	$= 1.750$	----- 1
0.750×2	$= 1.50$	----- 1
0.50×2	$= 1.00$	----- 1

It is an fractional part the carry is taken from top to bottom is 0111

$$\text{Thus } (0.4375)_{10} = (0.0111)_2$$

EXAMPLE 3: Convert the decimal number 43.375 to equivalent binary number

Answer: It consists of integer part (i.e.) 43 & fractional part (i.e.) 0.375

For integer part (i.e.) 43

It is integer part then Divide the given decimal number repeated by 2 and writing down the remainder after each Division.

Division	Remainder
2 43	
2 21	→ 1
2 10	→ 1
2 5	→ 0
2 2	→ 1
2 1	→ 0
0	→ 1

It is an integer part the remainder is taken from bottom to top is 101011

$$(43)_{10} = (101011)_2$$

For fractional part (i.e.) 0.375

It is a Fractional part then multiplies the given decimal number repeatedly by 2 each time recording carry.

Multiplication	product	carry
0.375×2	$= 0.750$	----- 0
0.750×2	$= 1.50$	----- 1
0.50×2	$= 1.00$	----- 1

It is an fractional part the carry is taken from top to bottom is 011

$$\text{Thus } (0.375)_{10} = (0.011)_2$$

The final answer is $(43.375)_{10} = (101011.011)_2$

Example: 4 convert the decimal number 282.0 to equivalent binary number.

Answer: It consists of integer part (i.e.) 282 & fractional part (i.e.) 0.0

For integer part (i.e.) 282

It is integer part then Divide the given decimal number repeated by 2 and writing down the remainder after each division.

Division	Remainder
2 282	
2 141	→ 0
2 70	→ 1
2 35	→ 0
2 17	→ 1
2 8	→ 1
2 4	→ 0
2 2	→ 0
2 1	→ 0
0	→ 1

It is an integer part the remainder is taken from bottom to top is 100011010

$$(282)_{10} = (100011010)_2$$

for fractional part (i.e.) 0.0

It is a Fractional part then multiplies the given decimal number repeatedly by 2 each time recording carry.

Multiplication	product	carry
0.0 x 2	= 0.00	----- 0

It is an fractional part the carry is taken from top to bottom is 0

$$(0.0)_{10} = (0)_2$$

Final answer is: $(282.0)_{10} = (100011010.0)_2$

EXAMPLE 5:

Convert the decimal number 1024 to equivalent binary number.

Answer:

It is integer part then Divide the given decimal number repeated by 2 and writing down the remainder after each Division

Division	Remainder
2 1024	
2 512	→ 0
2 256	→ 0
2 128	→ 0
2 64	→ 0
2 32	→ 0
2 16	→ 0
2 8	→ 0
2 4	→ 0
2 2	→ 0
2 1	→ 0
0	→ 1

It is an integer part the remainder is taken from bottom to top is

$$10000000000$$

$$(1024)_{10} = (10000000000)_2$$

EXAMPLE:6

Convert the decimal number 0.65 to equivalent binary number.

Answer:

It is a Fractional part then multiplies the given decimal number repeatedly by 2 each time recording carry.

Multiplication	product	carry
0.65 x 2	= 1.30	----- 1
0.30 x 2	= 0.60	----- 0
0.60 x 2	= 1.20	----- 1
0.20 x 2	= 0.40	----- 0
0.40 x 2	= 0.80	----- 0

The fraction may never terminated so stopped the multiplication

It is a fractional part the carry is taken from top to bottom is 10100...

$$\text{Thus } (0.65)_{10} = (10100\dots)_2$$

3.3 Convert Binary number into Decimal number:

➤ For Integer:

We can convert a binary number to its decimal equivalent by multiplying each binary digit with its position weight and sum of all bits gives the decimal number.

➤ For Fraction: It can be done in two steps.

Step-1: Multiplying the digits which lie after the decimal point by $2^{-1}, 2^{-2}, 2^{-3} \dots$

Step-2: Simplifying the resulting fractions and adding them to get decimal number.

EXAMPLE 1:

Convert the binary number 100101 to equivalent decimal number.

It is an integer part so we can multiply each binary digit with its position weight and sum of all bits gives the decimal number.

POSITION	5	4	3	2	1	0
VALUE(WEIGHTS)	2^5	2^4	2^3	2^2	2^1	2^0
BINARY POINT	1	0	0	1	0	1

$$\begin{aligned}(100101)_2 &= (1 \times 2^5) + (0 \times 2^4) + (0 \times 2^3) + (1 \times 2^2) + (0 \times 2^1) + (1 \times 2^0) \\ &= 32 + 0 + 0 + 4 + 0 + 1 \\ &= 37\end{aligned}$$

$$(100101)_2 = (37)_{10}$$

EXAMPLE 2:

Convert the binary number 0.111 to equivalent decimal number

Answer: It is a fractional part it can be done in two steps.

Step-1: Multiplying the digits which lie after the decimal point by $2^{-1}, 2^{-2}, 2^{-3} \dots$

Step-2: Simplifying the resulting fractions and adding them to get decimal number.

$$\begin{aligned}(0.111)_2 &= (1 \times 2^{-1}) + (1 \times 2^{-2}) + (1 \times 2^{-3}) \\ &= \frac{1}{2} + \frac{1}{4} + \frac{1}{8} \\ &= \frac{4 + 2 + 1}{8} \\ &= \frac{7}{8} \\ &= 0.875\end{aligned}$$

$$(0.111)_2 = (0.875)_{10}$$

EXAMPLE 3:

Convert the binary number 101101.101 to decimal number.

Answer: It consists of integer part (i.e.) 1101 & fractional part (i.e.) 0.101

For integer part (i.e.) 101101:

It is an integer part so we can multiply each binary digit with its position weight and sum of all bits gives the decimal number.

POSITION	5	4	3	2	1	0
VALUE(WEIGHTS)	2^5	2^4	2^3	2^2	2^1	2^0
BINARY POINT	1	0	1	1	0	1

$$\begin{aligned}
(101101)_2 &= (1 \times 2^5) + (0 \times 2^4) + (1 \times 2^3) + (1 \times 2^2) + (0 \times 2^1) + (1 \times 2^0) \\
&= (1 \times 32) + (0 \times 16) + (1 \times 8) + (1 \times 4) + (0 \times 2) + (1 \times 1) \\
&= 32 + 0 + 8 + 4 + 0 + 1 \\
&= 45 \\
(101101)_2 &= (45)_{10}
\end{aligned}$$

For fractional part (i.e.) 0.101:

It is a fractional part it can be done in two steps.

Step-1: Multiplying the digits which lie after the decimal point by $2^{-1}, 2^{-2}, 2^{-3}, \dots$

Step-2: Simplifying the resulting fractions and adding them to get decimal number

$$\begin{aligned}
(0.101)_2 &= (1 \times 2^{-1}) + (0 \times 2^{-2}) + (1 \times 2^{-3}) \\
&= \frac{1}{2} + 0 + \frac{1}{8} \\
&= \frac{4 + 0 + 1}{8} \\
&= \frac{5}{8} \\
&= 0.625
\end{aligned}$$

$$(0.111)_2 = (0.625)_{10}$$

The final answer is $(101101.101)_2 = (45.625)_{10}$

EXAMPLE 4: Convert the binary number 100101.0 to decimal number

Answer: It consists of integer part (i.e.) 100101 & fractional part (i.e.) 0.0

□ For integer part (i.e.) 100101:

It is an integer part so we can multiply each binary digit with its position weight and sum of all bits gives the decimal number.

POSITION	5	4	3	2	1	0
VALUE(WEIGHTS)	2^5	2^4	2^3	2^2	2^1	2^0
BINARY POINT	1	0	0	1	0	1

$$\begin{aligned}
(100101)_2 &= (1 \times 2^5) + (0 \times 2^4) + (0 \times 2^3) + (1 \times 2^2) + (0 \times 2^1) + (1 \times 2^0) \\
&= (1 \times 32) + (0 \times 16) + (0 \times 8) + (1 \times 4) + (0 \times 2) + (1 \times 1) \\
&= 32 + 0 + 0 + 4 + 0 + 1 \\
&= 37
\end{aligned}$$

$$(100101)_2 = (37)_{10}$$

□ For fractional part (i.e.) 0.0

It is a fractional part it can be done in two steps.

Step-1: Multiplying the digits which lie after the decimal point by $2^{-1}, 2^{-2}, 2^{-3}, \dots$

Step-2: Simplifying the resulting fractions and adding them to get decimal number

$$\begin{aligned}
(0.0)_2 &= (0 \times 2^{-1}) \\
&= 0 \\
(0.0)_2 &= (0)_{10}
\end{aligned}$$

The final answer is $(100101.0)_2 = (37.0)_{10}$

3.4 Convert binary number into hexadecimal number:

METHOD -1 for converting a binary number to its hexadecimal form first we convert binary number to decimal number and then convert decimal number to hexadecimal number.

METHOD-2

For INTEGER PART:

STEP-1: Divide the binary digits into groups of four (from RIGHT TO LEFT)

STEP-2: Convert each group of 4 binary digits to its hexadecimal equivalent

If any group does not have 4 bits it can be extended by adding 0's.

For integer part 0's can be added on left side of group

FOR FRACTIONAL PART:

STEP-1: Divide the binary digits into groups of four (from LEFT TO RIGHT)

STEP-2: Convert each group of 4 binary digits to its hexadecimal equivalent

If any group does not have 4 bits it can be extended by adding 0's

For fractional part 0's can be added on right side of group

EXAMPLE: Convert binary number 101110.100010 to hexadecimal number.

ANSWER:

METHOD-1

It consists of integer part (i.e.) 101110 & fractional part (i.e.) 0.100010

➤ **For integer part (i.e.) 101110:**

Binary to decimal: $(101110)_2 = (?)_{10}$

It is an integer part so we can multiply each binary digit with its position weight and sum of all bits gives the decimal number.

POSITION	5	4	3	2	1	0
VALUE(WEIGHTS)	2^5	2^4	2^3	2^2	2^1	2^0
DIGITS	1	0	1	1	1	0

$$\begin{aligned} (101110)_2 &= (1 \times 2^5) + (0 \times 2^4) + (1 \times 2^3) + (1 \times 2^2) + (1 \times 2^1) + (0 \times 2^0) \\ &= (1 \times 32) + (0 \times 16) + (1 \times 8) + (1 \times 4) + (1 \times 2) + (0 \times 1) \\ &= 32 + 0 + 8 + 4 + 2 + 0 \\ &= 46 \end{aligned}$$

$$(101110)_2 = (46)_{10}$$

Finally Decimal to hexadecimal: $(46)_{10} = (?)_{16}$

It is integer part then Divide the given decimal number repeated by 16 and writing down the remainder after each division.

Division		Remainder
16	46	
16	2	→ 14
	0	→ 2

It is an integer part the remainder is taken from bottom to top is 214

$$(46)_{10} = (214)_{16}$$

$$(46)_{10} = (2E)_{16} \quad (E=14)$$

Final answer for integer part $(101110)_2 = (46)_{10} = (2E)_{16}$

➤ **For fractional part (i.e.) 0.100010**

BINARY TO DECIMAL: $(0.100010)_2 = (?)_{10}$

It is a fractional part it can be done in two steps.

Step-1: Multiplying the digits which lie after the decimal point by $2^{-1}, 2^{-2}, 2^{-3}, \dots$

Step-2: Simplifying the resulting fractions and adding them to get decimal number

$$(0.100010)_2 = (1 \times 2^{-1}) + (0 \times 2^{-2}) + (0 \times 2^{-3}) + (0 \times 2^{-4}) + (1 \times 2^{-5}) + (0 \times 2^{-6})$$

$$= \frac{1}{2} + 0 + 0 + 0 + \frac{1}{32} + 0$$

$$= \frac{16+1}{32}$$

$$= \frac{17}{32}$$

$$= 0.53125$$

$$= 0.53125$$

$$(0.100010)_2 = (0.53125)_{10}$$

FINALLY DECIMAL TO HEXADECIMAL: $(0.53125)_{10} = (?)_{16}$

It is a Fractional part then multiplies the given decimal number repeatedly by 16 each time recording carry.

Multiplication		product		carry
0.53125 x 16	=	8.5	-----	8
0.5 x 16	=	8.0	-----	8
0.0 x 16	=	0.00	-----	0

It is a fractional part the carry is taken from top to bottom is 880

Final answer for fractional part $(0.53125)_{10} = (0.880)_{16}$

$$(101110.100010)_2 = (46.53125)_{10} = (2E.880)_{16}$$

METHOD-2

FOR INTEGER PART:

STEP-1: Divide the binary digits into groups of four (from RIGHT TO LEFT)

STEP-2: Convert each group of 4 binary digits to its hexadecimal equivalent

If any group does not have 4 bits it can be extended by adding 0's

For integer part 0's can be added on left side of group

FOR FRACTIONAL PART:

STEP-1: Divide the binary digits into groups of four (from LEFT TO RIGHT)

STEP-2: Convert each group of 4 binary digits to its hexadecimal equivalent

If any group does not have 4 bits it can be extended by adding 0's

For fractional part 0's can be added on right side of group

$$101110.100010 = (0010) (1110) . (1000) (1000)$$

$$= (2) (E) . (8) (8)$$

$$(101110.100010)_2 = (2E.88)_{16}$$

3.5 CONVERT HEXADECIMAL TO BINARY NUMBER

Method-1: Given hexadecimal first convert into decimal and then convert it into the Binary number.

Method-2: To convert a hexadecimal to its binary form each digit of the given should be converted In to the 4 bit binary.

EXAMPLE: convert the hexadecimal number FB2.1CE8 to binary number.

Answer: method-1

First convert the given hexadecimal into decimal and then convert it into the Binary number.

It consists of integer part (i.e.) FB2 & fractional part (i.e.) 0.1CE8

➤ **For integer part (i.e.) FB2**

FIRST HEXADECIMAL to decimal: $(FB2)_{16} = (?)_{10}$

It is an integer part so we can multiply each binary digit with its position weight and sum of all bits gives the decimal number.

POSITION	2	1	0
VALUE(WEIGHTS)	16^2	16^1	16^0
DIGITS	F	B	2

$$\begin{aligned}
 (FB2)_{16} &= (F \times 16^2) + (B \times 16^1) + (2 \times 16^0) \\
 &= (F \times 256) + (B \times 16) + (2 \times 1) \\
 &= (15 \times 256) + (11 \times 16) + (2 \times 1) \quad (F=15, B=11) \\
 &= 3840 + 176 + 2 \\
 &= 4018
 \end{aligned}$$

$$(FB2)_{16} = (4018)_{10}$$

➤ **Finally decimal to binary**

It is integer part then Divide the given decimal number repeatedly by 2 and writing down the remainder after each Division

Division	Remainder
2 4018	0
2 2009	1
2 1004	0
2 502	0
2 251	1
2 125	1
2 62	0
2 31	1
2 15	1
2 7	1
2 3	1
2 1	1
0	1

It is an integer part the remainder is taken from bottom to top is 111110110010

$$(4018)_{10} = (111110110010)_2$$

FINAL ANSWER FOR INTEGER PART: $(FB2)_{16} = (4018)_{10} = (111110110010)_2$

➤ **FOR FRACTIONAL PART (i.e.) 0.1CE8:**

HEXA DECIMAL TO DECIMAL NUMBER

For fractional part it can be done in two steps.

Step-1: Multiplying the digits which lie after the decimal point by $16^{-1}, 16^{-2}, 16^{-3}, \dots$

Step-2: Simplifying the resulting fractions and adding them to get decimal number.

$$\begin{aligned}
 (0.1CE8)_2 &= (1 \times 16^{-1}) + (C \times 16^{-2}) + (E \times 16^{-3}) + (8 \times 16^{-4}) \\
 &= 1/16 + C/256 + E/4096 + 8/65536 \\
 &= 1/16 + 12/256 + 14/4096 + 8/65536 \quad (C=12, E=14) \\
 &= 4096 + 3072 + 224 + 8 \\
 &\quad 65536 \\
 &= 7400/65536 \\
 &= 0.1129
 \end{aligned}$$

$$(0.1CE8)_2 = (0.1129)_{10}$$

FINALLY DECIMAL TO BINARY:

It is a Fractional part then multiplies the given decimal number repeatedly by 2 each time recording carry.

Multiplication	product	carry
0.1129 x 2	= 0.2258	----- 0
0.2258 x 2	= 0.4516	----- 0
0.4516 x 2	= 0.9032	----- 0

$$0.9032 \times 2 = 1.8064 \text{ ----- } 1$$

$$0.8064 \times 2 = 1.6128 \text{ ----- } 1$$

➤ The fraction may never terminated so stopped the multiplication

It is a fractional part the carry is taken from top to bottom is 00011...

$$\text{Thus } (0.1129)_{10} = (0.00011\dots)_2$$

$$\text{FOR fractional part: } (0.1CE8)_{16} = (0.1129)_{10} = (0.00011\dots)_2$$

$$\text{FINAL ANSWER: } (FB2.1CE8)_{16} = (4018.1129)_{10} = (111110110010.00011\dots)_2$$

Answer: method-2

To convert a hexadecimal to its binary form each digit of the given hexadecimal should be converted to its 4 bit binary equivalent & combine into a single binary number

FOR INTEGER PART(i.e.) FB2	FOR FRACTIONAL PART(i.e.) 0.1CE8
$(F)_{16} = (15)_{10} = (1111)_2$	$(1)_{16} = (1)_{10} = (0001)_2$
$(B)_{16} = (11)_{10} = (1011)_2$	$(C)_{16} = (12)_{10} = (1010)_2$
$(2)_{16} = (2)_{10} = (0010)_2$	$(E)_{16} = (14)_{10} = (1110)_2$
All the source taken from table	$(8)_{16} = (8)_{10} = (1000)_2$
$(FB2)_{16} = (111110110010)_2$	All the source taken from table
	$(0.1CE8)_{16} = (0.0001101011101000)_2$
FINAL ANSWER: $(FB2.1CE8)_{16} = (111110110010.0001101011101000)_2$	

Coding schemes Introduction

A Computer accepts and processes data in binary form. The process of converting data into binary form is called encoding of data. So we use some codes to represent characters in terms of 0's and 1's.

The most widely used codes are as follows:

1. Binary coded Decimal (BCD).
2. American Standard code for Information Interchange (ASCII).
3. Extended Binary Coded Decimal Interchange Code (EBCDIC).

1. Binary Coded Decimal (BCD): The BCD is the simplest binary code to represent a decimal number.

In BCD code each decimal digit is represented by four binary bits.

Decimal Digit	BCD Equivalent 8421
0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001

3.6 Explain the ASCII coding Scheme

The ASCII (**American Standard Code for Information Interchange**) is pronounced as "ask-ee".

- It was developed by American National Standards Institute (**ANSI**).
- It is very widely used code in small computers. The first ASCII code was 7-bit code but was later modified to an 8-bit code. It is a standard code to represent **alphanumeric data**.
 - **ASCII-7** is a 7-bit standard allows 2^7 combinations. 128 unique symbols are represented using ASCII-7. ASCII-7 has been modified by IBM to ASCII-8.
 - **ASCII-8** is an extended version of ASCII-7. ASCII-8 is an 8-bit standard allows 2^8 combinations. 256 unique symbols are represented using ASCII-8

Decimal	Hex	Oct	Character	Decimal	Hex	Oct	Character	Decimal	Hex	Oct	Character
32	20	040	space	64	40	100	@	96	60	140	ˆ
33	21	041	!	65	41	101	A	97	61	141	a
34	22	042	"	66	42	102	B	98	62	142	b
35	23	043	#	67	43	103	C	99	63	143	c
36	24	044	\$	68	44	104	D	100	64	144	d
37	25	045	%	69	45	105	E	101	65	145	e
38	26	046	&	70	46	106	F	102	66	146	f
39	27	047	'	71	47	107	G	103	67	147	g
40	28	050	(72	48	110	H	104	68	150	h
41	29	051)	73	49	111	I	105	69	151	i
42	2A	052	*	74	4A	112	J	106	6A	152	j
43	2B	053	+	75	4B	113	K	107	6B	153	k
44	2C	054	,	76	4C	114	L	108	6C	154	l
45	2D	055	-	77	4D	115	M	109	6D	155	m
46	2E	056	.	78	4E	116	N	110	6E	156	n
47	2F	057	/	79	4F	117	O	111	6F	157	o
48	30	060	0	80	50	120	P	112	70	160	p
49	31	061	1	81	51	121	Q	113	71	161	q
50	32	062	2	82	52	122	R	114	72	162	r
51	33	063	3	83	53	123	S	115	73	163	s
52	34	064	4	84	54	124	T	116	74	164	t
53	35	065	5	85	55	125	U	117	75	165	u
54	36	066	6	86	56	126	V	118	76	166	v
55	37	067	7	87	57	127	W	119	77	167	w
56	38	070	8	88	58	130	X	120	78	170	x
57	39	071	9	89	59	131	Y	121	79	171	y
58	3A	072	:	90	5A	132	Z	122	7A	172	z
59	3B	073	;	91	5B	133	[123	7B	173	{
60	3C	074	<	92	5C	134	\	124	7C	174	
61	3D	075	=	93	5D	135]	125	7D	175	}
62	3E	076	>	94	5E	136	^	126	7E	176	~
63	3F	077	?	95	5F	137	_	127	7F	177	DEL

We can check the value of any ASCII code by just holding down the ALT key and typing the ASCII code
Example: when we hold down the ALT key and type 66 from the keyboard, then the character B appears On the screen.

3.7 Explain the EBCDIC coding Scheme

EBCDIC is pronounced as "ebb-seedick".

- It is extended form of BCD code which is 8 bit. It is used extensively in large computers. **Extended Binary Coded Decimal Interchange Code** (EBCDIC) uses 8 bits to represent a symbol in the data.
- It is an **8 bit code** developed by **IBM** in 1964. It supports 256 characters. EBCDIC uses more or less the same characters as ASCII, but different code points. It has non-sequence letter format.
- EBCDIC codes are mainly used in the mainframe computers
- EBCDIC allows $2^8 = 256$ combinations of bits.
- It represents alphabets, decimal digits.

BELOW IS A ASCII TABLE

Dec	Hx	Oct	Char	Dec	Hx	Oct	Html	Chr	Dec	Hx	Oct	Html	Chr	Dec	Hx	Oct	Html	Chr
0	0	000	NUL (null)	32	20	040	 	Space	64	40	100	@	@	96	60	140	`	`
1	1	001	SOH (start of heading)	33	21	041	!	!	65	41	101	A	A	97	61	141	a	a
2	2	002	STX (start of text)	34	22	042	"	"	66	42	102	B	B	98	62	142	b	b
3	3	003	ETX (end of text)	35	23	043	#	#	67	43	103	C	C	99	63	143	c	c
4	4	004	EOT (end of transmission)	36	24	044	$	\$	68	44	104	D	D	100	64	144	d	d
5	5	005	ENQ (enquiry)	37	25	045	%	%	69	45	105	E	E	101	65	145	e	e
6	6	006	ACK (acknowledge)	38	26	046	&	&	70	46	106	F	F	102	66	146	f	f
7	7	007	BEL (bell)	39	27	047	'	'	71	47	107	G	G	103	67	147	g	g
8	8	010	BS (backspace)	40	28	050	((72	48	110	H	H	104	68	150	h	h
9	9	011	TAB (horizontal tab)	41	29	051))	73	49	111	I	I	105	69	151	i	i
10	A	012	LF (NL line feed, new line)	42	2A	052	*	*	74	4A	112	J	J	106	6A	152	j	j
11	B	013	VT (vertical tab)	43	2B	053	+	+	75	4B	113	K	K	107	6B	153	k	k
12	C	014	FF (NP form feed, new page)	44	2C	054	,	,	76	4C	114	L	L	108	6C	154	l	l
13	D	015	CR (carriage return)	45	2D	055	-	-	77	4D	115	M	M	109	6D	155	m	m
14	E	016	SO (shift out)	46	2E	056	.	.	78	4E	116	N	N	110	6E	156	n	n
15	F	017	SI (shift in)	47	2F	057	/	/	79	4F	117	O	O	111	6F	157	o	o
16	10	020	DLE (data link escape)	48	30	060	0	0	80	50	120	P	P	112	70	160	p	p
17	11	021	DC1 (device control 1)	49	31	061	1	1	81	51	121	Q	Q	113	71	161	q	q
18	12	022	DC2 (device control 2)	50	32	062	2	2	82	52	122	R	R	114	72	162	r	r
19	13	023	DC3 (device control 3)	51	33	063	3	3	83	53	123	S	S	115	73	163	s	s
20	14	024	DC4 (device control 4)	52	34	064	4	4	84	54	124	T	T	116	74	164	t	t
21	15	025	NAK (negative acknowledge)	53	35	065	5	5	85	55	125	U	U	117	75	165	u	u
22	16	026	SYM (synchronous idle)	54	36	066	6	6	86	56	126	V	V	118	76	166	v	v
23	17	027	ETB (end of trans. block)	55	37	067	7	7	87	57	127	W	W	119	77	167	w	w
24	18	030	CAN (cancel)	56	38	070	8	8	88	58	130	X	X	120	78	170	x	x
25	19	031	EM (end of medium)	57	39	071	9	9	89	59	131	Y	Y	121	79	171	y	y
26	1A	032	SUB (substitute)	58	3A	072	:	:	90	5A	132	Z	Z	122	7A	172	z	z
27	1B	033	ESC (escape)	59	3B	073	;	;	91	5B	133	[[123	7B	173	{	{
28	1C	034	FS (file separator)	60	3C	074	<	<	92	5C	134	\	\	124	7C	174	|	
29	1D	035	GS (group separator)	61	3D	075	=	=	93	5D	135]]	125	7D	175	}	}
30	1E	036	RS (record separator)	62	3E	076	>	>	94	5E	136	^	^	126	7E	176	~	~
31	1F	037	US (unit separator)	63	3F	077	?	?	95	5F	137	_	_	127	7F	177		DEL

Below is a EBCDIC TABLE

Dec	Hx	Oct	Char	Dec	Hx	Oct	Char	Dec	Hx	Oct	Char	Dec	Hx	Oct	Char
0	0	000	nul	(Null)	65	41	101	130	82	202	b	195	c3	303	C
1	1	001	soh	(Start of Heading)	66	42	102	131	83	203	c	196	c4	304	D
2	2	002	stx	(Start of Text)	67	43	103	132	84	204	d	197	c5	305	E
3	3	003	etx	(End of Text)	68	44	104	133	85	205	e	198	c6	306	F
4	4	004	pf	(Punch Off)	69	45	105	134	86	206	f	199	c7	307	G
5	5	005	ht	(Horizontal Tab)	70	46	106	135	87	207	g	200	c8	310	H
6	6	006	lc	(Lower Case)	71	47	107	136	88	210	h	201	c9	311	I
7	7	007	del	(Delete)	72	48	110	137	89	211	i	202	ca	312	
8	8	010	ge		73	49	111	138	8a	212		203	cb	313	
9	9	011	rif		74	4a	112	139	8b	213		204	cc	314	
10	a	012	smm	(Start of Manual Message)	75	4b	113	140	8c	214		205	cd	315	
11	b	013	vt	(Vertical Tab)	76	4c	114	141	8d	215		206	ce	316	
12	c	014	ff	(Form Feed)	77	4d	115	142	8e	216		207	cf	317	
13	d	015	cr	(Carriage Return)	78	4e	116	143	8f	217		208	d0	320	}
14	e	016	so	(Shift Out)	79	4f	117	144	90	220		209	d1	321	J
15	f	017	si	(Shift in)	80	50	120	145	91	221	j	210	d2	322	K
16	10	020	dle	(Data Link Escape)	81	51	121	146	92	222	k	211	d3	323	L
17	11	021	dc1	(Device Control 1)	82	52	122	147	93	223	l	212	d4	324	M
18	12	022	dc2	dc2 (Device Control 2)	83	53	123	148	94	224	m	213	d5	325	N
19	13	023	tm	(Tape Mark)	84	54	124	149	95	225	n	214	d6	326	O
20	14	024	res	(Restore)	85	55	125	150	96	226	o	215	d7	327	P
21	15	025	nl	(New Line)	86	56	126	151	97	227	p	216	d8	330	Q
22	16	026	bs	(Backspace)	87	57	127	152	98	230	q	217	d9	331	R
23	17	027	il	(Idle)	88	58	130	153	99	231	r	218	da	332	
24	18	030	can	(Cancel)	89	59	131	154	9a	232		219	db	333	
25	19	031	em	(End of Medium)	90	5a	132	155	9b	233		220	dc	334	
26	1a	032	cc	(Cursor Control)	91	5b	133	156	9c	234		221	dd	335	
27	1b	033	cu1	(Customer Use 1)	92	5c	134	157	9d	235		222	de	336	
28	1c	034	ifs	(Interchange File Separator)	93	5d	135	158	9e	236		223	df	337	
29	1d	035	igs	(Interchange Group Separator)	94	5e	136	159	9f	237		224	e0	340	\
30	1e	036	irs	(Interchange Record Separator)	95	5f	137	160	a0	240		225	e1	341	
31	1f	037	ius	(Interchange Unit Separator)	96	60	140	161	a1	241	~	226	e2	342	S
32	20	040	ds	(Digit Select)	97	61	141	162	a2	242	s	227	e3	343	T
33	21	041	sos	(Start of Significance)	98	62	142	163	a3	243	t	228	e4	344	U
34	22	042	fs	(Field Separator)	99	63	143	164	a4	244	u	229	e5	345	V
35	23	043			100	64	144	165	a5	245	v	230	e6	346	W
36	24	044	byp	(Bypass)	101	65	145	166	a6	246	w	231	e7	347	X
37	25	045	lf	(Line Feed)	102	66	146	167	a7	247	x	232	e8	350	Y
38	26	046	etb	(End of Transmission Block)	103	67	147	168	a8	250	y	233	e9	351	Z
39	27	047	esc	(Escape)	104	68	150	169	a9	251	z	234	ea	352	
40	28	050			105	69	151	170	aa	252		235	eb	353	
41	29	051			106	6a	152	171	ab	253		236	ec	354	
42	2a	052	sm	(Set Mode)	107	6b	153	172	ac	254		237	ed	355	
43	2b	053	cu2	(Customer Use 2)	108	6c	154	173	ad	255		238	ee	356	
44	2c	054			109	6d	155	174	ae	256		239	ef	357	
45	2d	055	enq	(Enquiry)	110	6e	156	175	af	257		240	f0	360	0
46	2e	056	ack	(Acknowledge)	111	6f	157	176	b0	260		241	f1	361	1
47	2f	057	bel	(Bell)	112	70	160	177	b1	261		242	f2	362	2
48	30	060			113	71	161	178	b2	262		243	f3	363	3
49	31	061			114	72	162	179	b3	263		244	f4	364	4
50	32	062	syn	(Synchronous Idle)	115	73	163	180	b4	264		245	f5	365	5
51	33	063			116	74	164	181	b5	265		246	f6	366	6
52	34	064	pn	(Punch On)	117	75	165	182	b6	266		247	f7	367	7
53	35	065	rs	(Reader Stop)	118	76	166	183	b7	267		248	f8	370	8
54	36	066	uc	(Upper Case)	119	77	167	184	b8	270		249	f9	371	9
55	37	067	eot	(End of Transmission)	120	78	170	185	b9	271		250	fa	372	
56	38	070			121	79	171	186	ba	272		251	fb	373	
57	39	071			122	7a	172	187	bb	273		252	fc	374	
58	3a	072			123	7b	173	188	bc	274		253	fd	375	
59	3b	073	cu3	(Customer Use 3)	124	7c	174	189	bd	275		254	fe	376	
60	3c	074	dc4	(Device Control 4)	125	7d	175	190	be	276		255	ff	377	eo
61	3d	075	nak	(Negative Acknowledge)	126	7e	176	191	bf	277					
62	3e	076			127	7f	177	192	c0	300	{				
63	3f	077	sub	(Substitute)	128	80	200	193	c1	301	A				
64	40	100	Sp	(Space)	129	81	201	194	c2	302	B				

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Other Systems

CONVERT OCTAL NUMBER INTO BINARY NUMBER:

Method-1: First we convert octal number into decimal and then decimal into binary.

Method-2: convert each digit of the given octal number into its 3-bit binary equivalent

Example: Convert the octal number 562 to equivalent binary number

Answer:

Method-1

First convert the given octal number into decimal and then convert it into the Binary number.

FIRST octal to decimal: $(562)_8 = (?)_{10}$

It is an integer part so we can multiply each binary digit with its position weight and sum of all bits gives the decimal number.

POSITION	2	1	0
VALUE(WEIGHTS)	8^2	8^1	8^0
DIGITS	5	6	2

$$\begin{aligned} (2AB)_8 &= (5 \times 8^2) + (6 \times 8^1) + (2 \times 8^0) \\ &= (5 \times 64) + (6 \times 8) + (2 \times 1) \\ &= (320) + (48) + (2) \\ &= 370 \end{aligned}$$

$$(2AB)_8 = (370)_{10}$$

➤ **Finally decimal to binary:** $(370)_{10} = (?)_2$

It is integer part then Divide the given decimal number repeated by 2 and writing down the Remainder after each Division

Division	Remainder
2 370	
2 185	→ 0
2 92	→ 1
2 46	→ 0
2 23	→ 0
2 11	→ 1
2 5	→ 1
2 2	→ 1
2 1	→ 0
2 0	→ 1

It is an integer part the remainder is taken from bottom to top is 101110010

$$(370)_{10} = (101110010)_2$$

FINAL ANSWER: $(562)_8 = (370)_{10} = (101110010)_2$

METHOD-2

Convert each digit of the given octal number into its 3-bit binary equivalent

$$(5)_8 = (5)_{10} = (101)_2$$

$$(6)_8 = (6)_{10} = (110)_2$$

$$(2)_8 = (2)_{10} = (010)_2$$

$$(562)_8 = (101110010)_2$$

CONVERT BINARY NUMBER INTO OCTAL NUMBER:

Method-1: To convert into octal number we need to

Convert binary into decimal and then convert decimal to octal number.

Method-2: FOR INTEGER PART:

STEP-1: Divide the binary digits into groups (from RIGHT TO LEFT)

STEP-2: Convert each group of 3 binary digits to its octal equivalent

If any group does not have 3 bits it can be extended by adding 0's

For integer part 0's can be added on left side of group

FOR FRACTIONAL PART:

STEP-1: Divide the binary digits into groups (from LEFT TO RIGHT)

STEP-2: Convert each group of 3 binary digits to its octal equivalent

If any group does not have 3 bits it can be extended by adding 0's

For fractional part 0's can be added on right side of group

EXAMPLE 1: Convert the binary number 1001110.0 to octal number

Answer:

Method-1

For converting a binary number to its octal form first we convert binary number to decimal number and then Convert decimal number to octal number.

It consists of integer part (i.e.) 1001110 & fractional part (i.e.) 0.0

➤ **For integer part (i.e.) 1001110**

Binary to decimal: $(1001110)_2 = (?)_{10}$

It is an integer part so we can multiply each binary digit with its position weight and sum of all bits gives the decimal number.

POSITION	6	5	4	3	2	1	0
VALUE(WEIGHTS)	2^6	2^5	2^4	2^3	2^2	2^1	2^0
DIGITS	1	0	0	1	1	1	0

$$\begin{aligned}
 (1001110)_2 &= (1 \times 2^6) + (0 \times 2^5) + (0 \times 2^4) + (1 \times 2^3) + (1 \times 2^2) + (1 \times 2^1) + (0 \times 2^0) \\
 &= (1 \times 64) + (0 \times 32) + (0 \times 16) + (1 \times 8) + (1 \times 4) + (1 \times 2) + (0 \times 1) \\
 &= 64 + 0 + 0 + 8 + 4 + 2 + 0 \\
 &= 78
 \end{aligned}$$

$$(1001110)_2 = (78)_{10}$$

Finally Decimal to octal number $(78)_{10} = (?)_8$

It is integer part then Divide the given decimal number repeated by 8 and writing down the remainder after each division.

Division	Remainder	
8	78	
8	9	→ 6
8	1	→ 1
	0	→ 1

It is an integer part the remainder is taken from bottom to top is 116

$$(78)_{10} = (116)_8$$

Final answer for integer part $(1001110)_2 = (78)_{10} = (116)_8$

➤ **For fractional part (i.e.) 0.0**

Binary to decimal: $(0.0)_2 = (?)_{10}$

It is a fractional part it can be done in two steps.

Step-1: Multiplying the digits which lie after the decimal point by $2^{-1}, 2^{-2}, 2^{-3}, \dots$

Step-2: Simplifying the resulting fractions and adding them to get decimal number.

$$\begin{aligned}
 (0.0)_2 &= (0 \times 2^{-1}) \\
 &= 0 \\
 (0.0)_2 &= (0.0)_{10}
 \end{aligned}$$

FINALLY DECIMAL TO OCTAL:

It is a Fractional part then multiplies the given decimal number repeatedly by 8 each time recording carry.

$$\begin{array}{r} \text{Multiplication} \quad \text{product} \quad \text{carry} \\ 0.0 \times 8 = 0.0 \quad \text{-----} \quad 0 \end{array}$$

It is a fractional part the carry is taken from top to bottom is 0

$$\text{Thus } (0.0)_{10} = (0.0)_8$$

$$\text{Final answer for fractional part } (0.0)_2 = (0.0)_{10} = (0.0)_8$$

THE FINAL ANSWER IS $(1001110.0)_2 = (78.0)_{10} = (116.0)_8$

METHOD-2

$$\begin{aligned} (1001110.0) &= (1) (001) (110). (0) \\ &= (001) (001) (110). (000) \\ &= (1) (1) (6) . (0) \\ (1001110.0)_2 &= (116.0)_8 \end{aligned}$$

CONVERT HEXADECIMAL INTO OCTAL NUMBER:

EXAMPLE 1: What is the result of the conversion $56.34_{(16)} = ?_{(8)}$

ANSWER: first we have to convert the hexadecimal into decimal number & then decimal number into octal

It consists of integer part (i.e.) 56 & fractional part (i.e.) 0.34

➤ **For integer part (i.e.) 56**

FIRST HEXADECIMAL to decimal: $(56)_{16} = (?)_{10}$

It is an integer part so we can multiply each binary digit with its position weight and sum of all bits gives the decimal number.

POSITION	1	0
VALUE(WEIGHTS)	16^1	16^0
DIGITS	5	6

$$\begin{aligned} (56)_{16} &= (5 \times 16^1) + (6 \times 16^0) \\ &= (5 \times 16) + (6 \times 1) \\ &= 80 + 6 \\ &= 86 \end{aligned}$$

$$(56)_{16} = (86)_{10}$$

Finally DECIMAL to OCTAL: $(86)_{10} = (?)_8$

It is integer part then Divide the given decimal number repeatedly by 8 and writing down the remainder after each Division

Division	Remainder
8	86
8	10
8	1
	0
	6
	2
	1

It is an integer part the remainder is taken from bottom to top is 126

$$(86)_{10} = (126)_8$$

FINAL ANSWER FOR INTEGER PART: $(56)_{16} = (86)_{10} = (126)_8$

➤ **FOR FRACTIONAL PART (i.e.) 0.34:**

FIRST HEXA DECIMAL TO DECIMAL NUMBER: $(0.34)_{16} = (?)_{10}$

For fractional part it can be done in two steps.

Step-1: Multiplying the digits which lie after the decimal point by $16^{-1}, 16^{-2}, 16^{-3} \dots$

Step-2: Simplifying the resulting fractions and adding them to get decimal number.

$$(0.34)_{16} = (3 \times 16^{-1}) + (4 \times 16^{-2})$$

$$\begin{aligned}
&= 3/16 + 4/256 \\
&= 3 \times 16 + 4 \\
&\quad 256 \\
&= 48 + 4 \\
&\quad 52 \\
&= 52/256 \\
&= 0.203125 \\
(0.34)_{16} &= (0.203125)_{10}
\end{aligned}$$

FINALLY DECIMAL TO OCTAL: $(0.203125)_{10} = (?)_8$

It is a Fractional part then multiplies the given decimal number repeatedly by 8 each time recording carry.

Multiplication	product	carry
0.203125 x 8	= 1.625	----- 1
0.625 x 8	= 5	----- 5

It is an fractional part the carry is taken from top to bottom is 15

Thus $(0.203125)_{10} = (0.15)_8$

FINAL ANSWER FOR fractional part: $(0.34)_{16} = (0.203125)_{10} = (0.15)_8$

FINAL ANSWER: $(56.34)_{16} = (86.203125)_{10} = (126.15)_8$

Concept of a byte and word

Bit: It is the smallest unit of information used in a computer system. It can have either the value 0 or 1

Nibble: It is a combination of 4 bits. Example: 0101

Byte: Byte is a group of 8 bits, Derived from words "by eight". Example: 11001100, 00011100

Word: combination of 16 bits (or) Group of 2 bytes. Example: 1111111100000000

Double Word: 32 bits.

KB (KILO BYTE): Used to represent 1024 bytes of information.

MB (MEGA BYTE): Used to represent 1024 KILO bytes of information.

Likewise GB, TB, PB, EB, ZB, YB

