# 7256 <br> BOARD DIPLOMA EXAMINATION, (C-20) FEBRUARY/MARCH - 2022 <br> DME - THIRD SEMESTER EXAMINATION <br> ENGINEERING MATHEMATICS - II 

Time : 3 hours ]
Total Marks : 80

## PART—A

$3 \times 10=30$

Instructions : (1) Answer all questions.
(2) Each question carries three marks.

1. Evaluate $\int(\cos x-\sin x) d x$
2. Evaluate $\int(3 x-5)^{7} d x$
3. Evaluate $\int \frac{1}{x(\log x)^{2}} d x$
4. Evaluate $\int x e^{-x} d x$
5. Evaluate $\int_{0}^{\frac{\pi}{4}} \sec ^{2} x d x$
6. Evaluate $\int_{0}^{\frac{\pi}{2}} \sin ^{5} x d x$
7. Find the mean value of $y=x^{2}$ in the interval $[2,3]$.
8. Form the differential equation by eliminating the arbitrary constants $A$ and $B$ from the equation $y=A e^{x}+B e^{-x}$.
9. Solve $\frac{d y}{d x}=\frac{\sqrt{1-y^{2}}}{\sqrt{1-x^{2}}}$
10. Show that the differential equation $\left(y^{2}-2 x y\right) d x-\left(x^{2}-2 x y\right) d y=0$ is exact.

## PART—B

Instructions: (1) Answer all questions.
(2) Each question carries eight marks.
11. (a) Evaluate $\int \sin ^{4} x \cos ^{3} x d x$

> (OR)
(b) Evaluate $\int \frac{x}{x^{2}+x-20} d x$
12. (a) Evaluate $\int \frac{1}{5+4 \sin x} d x$

## (OR)

(b) Evaluate $\int x^{3} \sin 5 x d x$
13. (a) Evaluate $\int_{0}^{1} \frac{5 x^{3}}{\sqrt{1-x^{8}}} d x$
(OR)
(b) Evaluate $\int_{0}^{\frac{\pi}{2}} \frac{\sqrt{\cos x}}{\sqrt{\sin x}+\sqrt{\cos x}} d x$
14. (a) Find the area enclosed between the parabolas $y^{2}=x$ and $x^{2}=y$.

## (OR)

(b) Find the RMS value of $f(x)=\sqrt{27-x^{2}}$ in the interval $[0,3]$.
15. (a) Find the volume of the solid generated by revolving the portion of the parabola $y^{2}=4 a x$ cut off by its latus rectum about the $x$-axis.

## (OR)

(b) Approximate the area under the curve $y=\frac{1}{x}$ between $x=1$ and $x=5$ using the trapezoidal rule with $n=4$ sub-intervals.

## PART—C

Instructions : (1) Answer the following question.
(2) The question carries ten marks.
16. Solve $\frac{d y}{d x}+\frac{y}{x}=y^{2}$

