# с20-снот-м-301

# 7256

## **BOARD DIPLOMA EXAMINATION, (C-20)**

### FEBRUARY/MARCH — 2022

### **DME - THIRD SEMESTER EXAMINATION**

ENGINEERING MATHEMATICS - II

*Time* : 3 hours ]

#### PART-A

[ Total Marks : 80

 $3 \times 10 = 30$ 

- **Instructions :** (1) Answer **all** questions.
  - (2) Each question carries three marks.
  - **1.** Evaluate  $\int (\cos x \sin x) dx$
  - **2.** Evaluate  $\int (3x-5)^7 dx$
  - **3.** Evaluate  $\int \frac{1}{x(\log x)^2} dx$
  - **4.** Evaluate  $\int xe^{-x} dx$
  - **5.** Evaluate  $\int_0^{\frac{\pi}{4}} \sec^2 x \, dx$
  - **6.** Evaluate  $\int_0^{\frac{\pi}{2}} \sin^5 x \, dx$
  - **7.** Find the mean value of  $y = x^2$  in the interval [2,3].

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8. Form the differential equation by eliminating the arbitrary constants A and B from the equation  $y = Ae^x + Be^{-x}$ .

9. Solve 
$$\frac{dy}{dx} = \frac{\sqrt{1-y^2}}{\sqrt{1-x^2}}$$

**10.** Show that the differential equation  $(y^2 - 2xy)dx - (x^2 - 2xy)dy = 0$  is exact.

#### PART-B

8×5=40

**Instructions :** (1) Answer **all** questions.

(2) Each question carries **eight** marks.

**11.** (a) Evaluate 
$$\int \sin^4 x \cos^3 x \, dx$$

(**O**R)

(b) Evaluate 
$$\int \frac{x}{x^2 + x - 20} dx$$

**12.** (a) Evaluate 
$$\int \frac{1}{5+4\sin x} dx$$

(OR)

(b) Evaluate 
$$\int x^3 \sin 5x \, dx$$

**13.** (a) Evaluate 
$$\int_0^1 \frac{5x^3}{\sqrt{1-x^8}} dx$$

(OR)

(b) Evaluate 
$$\int_{0}^{\frac{\pi}{2}} \frac{\sqrt{\cos x}}{\sqrt{\sin x} + \sqrt{\cos x}} dx$$

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[ Contd...

**14.** (a) Find the area enclosed between the parabolas  $y^2 = x$  and  $x^2 = y$ .

# (OR)

- (b) Find the RMS value of  $f(x) = \sqrt{27 x^2}$  in the interval [0,3].
- **15.** (a) Find the volume of the solid generated by revolving the portion of the parabola  $y^2 = 4ax$  cut off by its latus rectum about the *x*-axis.

#### (OR)

(b) Approximate the area under the curve  $y = \frac{1}{x}$  between x = 1 and x = 5 using the trapezoidal rule with n = 4 sub-intervals.

## PART-C

 $10 \times 1 = 10$ 

Instructions: (1) Answer the following question.

(2) The question carries **ten** marks.

**16.** Solve  $\frac{dy}{dx} + \frac{y}{x} = y^2$ 

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