C14-M/CHOT/RAC-401

4477

BOARD DIPLOMA EXAMINATION, (C-14) OCT/NOV—2018

DME—FOURTH SEMESTER EXAMINATION

ENGINEERING MATHEMATICS - III

Time: 3 Hours] [Total Marks: 80

PART—A

 $3 \times 10 = 30$

Instruction: (1) Answer all questions. Each question carries three marks.

- (2) Answers should be brief and straight to the point and shall not exceed **five** simple sentences.
- 1. Solve $(D^2 + 3D + 2)y = 0$
- 2. Solve $(D^3 2D^2 D + 2)y = 0$
- 3. Find the particular integral of $(D^2 5D + 6)y = e^{-2x}$
- **4.** Find the Laplace transform of $e^{-2t} 3\sin t + 2$
- 5. Find the Laplace transform of $e^{-t}\cos 2t$
- **6.** Find the Laplace transform of $t \sin 2t$
- 7. Find the inverse Laplace transform of $\frac{s}{(s+2)^2}$
- **8.** Write down the formulae for finding Euler's constants for f(x) in $(0, 2\pi)$.
- **9.** What is the value of b_n in the Fourier series expansion of f(x) = |x| in $(-\pi, \pi)$.
- 10. In an experiment of tossing 4 coins simultaneously, write the probability of successes for getting 2 heads.

Instruction: (1) Answer any five questions. Each question carries ten marks.

(2) Answers should be comprehensive and the criterion for valuation is the content but not the length of the answer.

11. (a) Solve
$$(D^2 - 5D + 6)y = 3e^{5x}$$

(b) Solve
$$(D^2 + 16)y = \cos 4x$$

12. (a) Solve
$$(D^2 - 2D + 2)y = e^{3x} + \sin 2x$$

(b) Solve
$$(D^2 - 4D + 4)y = 2x^3 - 1$$

13. (a) Find the Laplace transform of sin2tcost

(b) Find the Laplace transform of $t^2 \sin 3t$

14. (a) Evaluate $L\left\{\int_{0}^{t} e^{-4t} \sin 3t \ dt\right\}$

(b)
$$L^{-1}\left\{\frac{2s-5}{s^2-4}\right\}$$

15. Write down the Fourier series for $f(x) = x - x^2$ in the interval $-\pi < x < \pi$.

16. Find the Fourier series of the function f(x) = x in -2 < x < 2.

17. (a) A book contains 85 pages. A page is chosen at random. What is the probability that the sum of the digits on the page is 8.

(b) What is the chance that a leap year selected at random will contain 53 Sundays.

18. (a) When two dices are thrown, find the probability of getting the sum 6 or 7.

(b) A card is drawn at random from a normal pack of cards. What is the probability that it is either a spade or a queen.
