

C14-A-301/C14-AA-301/C14-AEI-301/ C14-CH-301/C14-CHST-301/C14-CHPC-301/ C14-CHPP-301/C14-CHOT-301/C14-PET-301/ C14-PCT-301/C14-C-301/C14-CM-301/C14-EC-301/ C14-EE-301/C14-IT-301/C14-M-301/C14-RAC-301/ C14-MET-301/C14-MNG-301//C14-TT-301/ C14-BM-301

## 4201

BOARD DIPLOMA EXAMINATION, (C-14) OCT/NOV—2017

## THIRD SEMESTER (COMMON) EXAMINATION

## ENGINEERING MATHEMATICS——II

Time : 3 hours ]

Instructions : (1) Answer all questions.
(2) Each question carries three marks.
(3) Answers should be brief and straight to the point and shall not exceed five simple sentences.

1. Evaluate

$$
\int\left(\sqrt[3]{x}-e^{x}+\sin x\right) d x
$$

2. Evaluate :

$$
\int \frac{1}{1-\sin x} d x
$$

3. Evaluate :

$$
\int \sec ^{2}(2 x+3) d x
$$

4. Evaluate :

$$
\int_{1}^{\sqrt{3}} \frac{1}{1+x^{2}} d x
$$

5. Evaluate :

$$
\int_{0}^{1} \frac{\sin ^{-1} x}{1-x^{2}} d x
$$

6. Find the differential equation by eliminating $a$ and $b$ form $y=a \tan ^{-1} x+b$.
7. Solve :

$$
\frac{d y}{d x}=\sqrt{\frac{1-y^{2}}{1-x^{2}}}
$$

8. Solve :

$$
\frac{d y}{d x}=e^{-x+y}+x^{2} e^{y}
$$

9. Find the Arithmetic mean from the following distribution :

| Wt. in kgs | 50 | 55 | 60 | 65 | 70 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. of men | 15 | 20 | 25 | 30 | 10 |

10. Find the median of the following distribution :

| Income (in ₹) | 120 | 160 | 90 | 220 | 260 | 190 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of persons | 24 | 26 | 16 | 20 | 6 | 30 |

## PART-B

Instructions : (1) Answer any five questions.
(2) Each question carries ten marks.
(3) Answers should be comprehensive and the criterion for valuation is the content but not the length of the answer.
11. (a) Evaluate :

$$
\int \sin 6 x \cos 2 x d x
$$

(b) Evaluate :

$$
\int \frac{\tan x-1}{\tan x+1} d x
$$

12. (a) Evaluate :

$$
\int \sin ^{4} \theta \cos ^{3} \theta d \theta
$$

(b) Evaluate :

$$
\int x \log x d x
$$

13. (a) Evaluate :

$$
\int x^{4} e^{2 x} d x
$$

(b) Evaluate :

$$
\int_{0}^{\pi / 2} \frac{\sin ^{20} x}{\sin ^{20} x+\cos ^{20} x} d x
$$

14. (a) Find the enclosed by the ellipse

$$
\frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}=1
$$

by the method of integration.
(b) Find the volume of a solid generated revolving the area enclosed between $x^{2}=y^{2}-3, x=1, x=2$, about $x$-axis.
15. (a) Find the RMS value of $\sqrt{\log x}$ over the range $x=1, x=e$.
(b) Find $\int_{1}^{2} \frac{1}{x} d x$ approximately by dividing the interval [1, 2] into 5 equal parts using trapezoidal rule.
16. (a) Find the differential equation of the family of curves $y=A \cos 3 x+B \sin 3 x$.
(b) Solve

$$
\frac{d y}{d x}+y=\cos x
$$

17. (a) Solve :

$$
\frac{d y}{d x}=\frac{x^{2}+y^{2}}{x y}
$$

(b) Solve :

$$
\left(3 x^{2}+4 y\right) d x+\left(4 x+3 y^{2}\right) d y=0
$$

18. From the marks obtained by 8 students in Mathematics and Statistics, compute the rank correlation coefficient :

| Student number | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Marks in Mathematics | 70 | 48 | 58 | 55 | 54 | 50 | 60 | 52 |
| Marks in Statistics | 62 | 47 | 53 | 60 | 55 | 68 | 51 | 48 |

