

C14-EE-401/C14-CHPP-401/ C14-PET-401

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BOARD DIPLOMA EXAMINATION, (C-14) MARCH/APRIL—2018 DEEE—FOURTH SEMESTER EXAMINATION

ENGINEERING MATHEMATICS-III

Time : 3 hours [Total Marks: 80

PART—A

 $3 \times 10 = 30$

- **Instructions:** (1) Answer **all** questions.
 - (2) Each question carries **three** marks.
 - (3) Answers should be brief and straight to the point and shall not exceed five simple sentences.
 - Solve $(D^2 6D + 4)y = 0$.
 - Solve $(D^3 2D^2 3D)y = 0$.
 - Find the particular integral of $(D^2+4)y=\cos 4x$. 3.
 - Find $L(\sin^2 2t)$.
 - Find $L(t^3e^{-5t})$.
 - Evaluate $\int_{0}^{\infty} e^{-4t} \cos 3t \ dt$
 - 7. Find $L^{-1}\left(\frac{1}{s(s+2)}\right)$.
 - Find the Fourier coefficient b_n for the function f(x)=x in the interval $(0,\pi)$.

- **9.** Write the Fourier series for the function f(x) defined in the interval $(c,c+2\pi)$.
- **10.** A bag contains 5 black, 7 red and 4 white balls. A ball is drawn at random. Find the probability that the ball drawn is white.

PART-B

 $10 \times 5 = 50$

Instructions: (1) Answer any five questions.

- (2) Each question carries ten marks.
- (3) Answers should be comprehensive and the criteria for valuation are the content but not the length of the answer.
- **11.** (a) Solve $\frac{d^2y}{dx^2} 2\frac{dy}{dx} + y = e^{3x} \sinh 2x$
 - (b) Solve $(D^3 + 4D)y = \cos 2x$
- **12.** (a) Solve $(D^2 4D + 3)y = x^2$
 - (b) Find the particular integral of $(D^2 + D 2)y = x + \sin x$
- **13.** (a) Find $L\left(\frac{1-\cos t}{t}\right)$.
 - (b) Find $\left(\int_{0}^{t} te^{-t} \sin t \, dt\right)$
- 14. Using Laplace transform method, solve

$$Y'''+2Y''-Y'-2Y=0$$
 given $Y(0)=Y'(0)=0$ and $Y'''(0)=6$.

15. Obtain the Fourier series of $f(x) = e^{ax}$ in the interval

$$-\pi < x < \pi$$
.

16. Find the Fourier series of the function f(x) given by f(x) = x-2 in the interval 0 to 2π .

- 17. (a) The probability for a contractor to get a road contract is $\frac{2}{3}$ and to get a building contract is $\frac{5}{9}$. The probability to get at least one contract is $\frac{4}{5}$. Find the probability that he gets the both the contracts.
 - (b) A card is selected at a random from a pack of cards. Let 'A' be the event that card is below 5 and 'B' be the event that the card is heart. Show that A and B are independent events.
- 18. There are two identical boxes containing respectively 3 blue, 2 red marbles; and 2 blue, 5 red marbles. A marble is drawn at random from one of the boxes turns out to be blue. What is the probability that it came from the first box?

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