## EC 23002 Digital Electronics Circuits (3-0-3 5)

## Pre- requisite: None

Switching algebra, minimizing functions using maps, different logic families, TTL, ECL, NMOS, CMOS, pass transistor logic, combinational logic circuits:- adders / subtractor, demultiplexers, encoders , decoders , ROMs, PLAs etc. sequential logic circuits:- flip flops and latches, shifters, counters, finite state machine - state transition diagrams and state transition tables. memory elements :- ROM, PROM, RAM-SRAM, DRAM. case studies : a simple computer, RTL - micro-instruction, instruction decoders timing and controller circuits, data path unit.

## Sector wise distribution:

1. Switching algebra, minimizing functions using maps
2. Different logic families, TTL, ECL, NMOS, CMOS, pass transistor logic
3. Combinational logic circuits:- adders / subtractor, demultiplexers, encoders , decoders , ROMs, PLAs etc.
4. Sequential logic circuits:- flip flops and latches , shifters, counters, finite state machine state transition diagrams and state transition tables.
5. Memory elements :- ROM, PROM, RAM-SRAM, DRAM.
6. Case studies : a simple computer, RTL - micro-instruction, instruction decoders timing and controller circuits, data path unit.

Books: Grinich Jackson, Tocci, Rabaey, Taub, Mano, Yarbrough, Malvino

| Roll No. | Name | Hall of Residence | Email id | CGPA |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |

[^0]
## Why Digital?

Digital : Processing of discretized information(signal).

1. Accurate.
2. Flexible.
3. It requires less operational energy.
4. Repeatability.
5. ?
6. ?

The foundation of any digital system is the logic gate. A variety of electronic circuits exists that can be used as basic logic gates. One logic family is built around one kind of basic circuit.

## Why Different Logic Families?

1. Space satellite, Digital wristwatch - low power consumption
2. Scientific Computer - high speed
3. Digital Control of equipment in industrial environment - noise immunity
4. Compatibility
5. Flexibility
6. Cost
7. Size, Packing Density
8. Evolution

Transistor-inverter is key to development of logic circuit. Why?
Diodes, Switches can be used to build OR and AND circuit but not NOT circuit. Hence, with these it is not possible to develop every type of logic circuits.


Can you get simpler diode circuits for same logic operations?

## A typical transistor inverter



Analysis:
Base current $\mathrm{I}_{\mathrm{B}}=0$ till $\mathrm{V}_{\mathrm{BE}}<0.7 \mathrm{~V}$ i.e. $\mathrm{V}_{\text {in }}<0.7 \mathrm{~V}$. Transistor is cut off and $\mathrm{I}_{\mathrm{C}}=0$ with $\mathrm{V}_{\text {out }}=5 \mathrm{~V}$ over entire range.

When $\mathrm{V}_{\text {in }}$ is increased beyond 0.7 V , base current begins to flow and the transistor moves from cut off region to normal active region. Hence, the coordinates $\mathrm{V}_{\text {in }}=0.7 \mathrm{~V}, \mathrm{~V}_{\text {out }}=5 \mathrm{~V}$ mark first transition point in the transfer function of this circuit. This is also termed as breakpoint or edge of cutoff (EOC).

Now, $\mathrm{I}_{\mathrm{B}}=\left(\mathrm{V}_{\text {in }}-\mathrm{V}_{\mathrm{BE}(\text { on })}\right) / \mathrm{R}_{\mathrm{B}}$

$$
\begin{aligned}
& \text { And } \mathrm{I}_{\mathrm{C}}=\beta_{\mathrm{F}} \mathrm{I}_{\mathrm{B}}: \text { as long as } \mathrm{V}_{\mathrm{CE}}<\mathrm{V}_{\mathrm{CE}(\text { sat })} \\
& \text { Or, } \mathrm{V}_{\text {out }}=\mathrm{V}_{\mathrm{CC}}-\beta_{\mathrm{F}} \mathrm{R}_{\mathrm{C}}\left(\mathrm{~V}_{\text {in }}-\mathrm{V}_{\mathrm{BE}(\text { on })}\right) / \mathrm{R}_{\mathrm{B}}
\end{aligned}
$$

Thus $\mathrm{V}_{\text {out }}$ decreases linearly with increase in $\mathrm{V}_{\text {in }}$ as long as transistor remains in active mode.
As $\mathrm{V}_{\text {in }}\left(\right.$ or $\left.\mathrm{I}_{\mathrm{B}}\right)$ is increased a second transition point is reached when $\mathrm{V}_{\text {out }}=\mathrm{V}_{\mathrm{CE}(\mathrm{sat})}$. The values of $\mathrm{I}_{\mathrm{C}}$ and $\mathrm{I}_{\mathrm{B}}$ for this condition (the subscript EOS means edge of sturation):
$\mathrm{I}_{\mathrm{C}(\mathrm{EOS})}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}(\text { sat })}\right) / \mathrm{R}_{\mathrm{C}}=(5-0.2) / 1=4.8 \mathrm{~mA} \quad$ and $\mathrm{I}_{\mathrm{B}(\mathrm{EOS})}=\mathrm{I}_{\mathrm{C}(\mathrm{EOS})} / \beta_{\mathrm{F}}=4.8 / 50=0.096 \mathrm{~mA}$
Then $\mathrm{V}_{\text {in(EOS })}=\mathrm{V}_{\mathrm{BE}(\text { on })}+\mathrm{I}_{\mathrm{B}(\mathrm{EOS})} \mathrm{R}_{\mathrm{B}}=0.7+(0.096)(10)=1.66 \mathrm{~V}$
Thus $\mathrm{V}_{\text {in }} \geq 1.66 \mathrm{~V}$ the transistor saturates. (Saturating Logic)

$\mathrm{V}_{\mathrm{IL}}=$ Threshold voltage for LOW level
$\mathrm{V}_{\mathrm{OL}}=$ Threshold voltage for LOW level
$\mathrm{V}_{\mathrm{IH}}=$ Threshold voltage for HIGH level $\mathrm{V}_{\mathrm{OH}}=$ Threshold voltage for HIGH level

For the input any voltage $<0.7 \mathrm{~V}$ is recognized as LOW input level
And any voltage $>1.66 \mathrm{~V}$ indicates HIGH input level.
At the input side voltage levels between 0.7 to 1.66 V are to be avoided because they lead to output voltage levels that are ambiguous.

Logic swing : The difference between the two output voltages $=\mathrm{V}_{\mathrm{OH}}-\mathrm{V}_{\mathrm{OL}}=5-0.2=4.8 \mathrm{~V}$

## Noise Margins

$\mathrm{NM}_{\mathrm{L}}$ : LOW level noise margin $=\mathrm{V}_{\mathrm{IL}}-\mathrm{V}_{\mathrm{OL}}=0.7-0.2=0.5 \mathrm{~V}$
$\mathrm{NM}_{\mathrm{H}}:$ HIGH level noise margin $=\mathrm{V}_{\mathrm{OH}}-\mathrm{V}_{\mathrm{IH}}=5.0-1.66=3.34 \mathrm{~V}$
Noise margin capability increases if $\mathrm{V}_{\mathrm{OH}}$ and $\mathrm{V}_{\mathrm{OL}}$ move away from each other i.e. with larger logic swing.

Noise margin capability increases if $\mathrm{V}_{\mathrm{IH}}$ and $\mathrm{V}_{\mathrm{IL}}$ move towards each other i.e. with narrower transition width.

Transition width $=\mathrm{V}_{\mathrm{IH}}-\mathrm{V}_{\mathrm{IL}}=1.66-0.7=0.96 \mathrm{~V}$


For LOW level input a noise generator of amplitude $\mathrm{NM}_{\mathrm{L}}(=0.5 \mathrm{~V})$ could be inserted in series at the input without having any effect on the output.

Similarly, for HIGH level input a noise generator of amplitude $\mathrm{NM}_{\mathrm{H}}(=3.34 \mathrm{~V})$ could be inserted in series at the input without having any effect on the output.

Note, the polarity of the two noise generator.

## Fan out

One logic gate generally is not operated in isolation. Connections are made from output of one to input of one or more similar circuits. The maximum number of such inputs that can be connected is known as fanout.


FIGURE 3.4
Transistor-inverter circuit with $n$ other inverter inputs as a load.

## Fanout Computation:

When A is HIGH, $\mathrm{Q}_{0}$ is saturated and F will be LOW.
With $\mathrm{V}_{\mathrm{CE}(\text { sat })}=0.2 \mathrm{~V}$ all the load gates will be in the OFF state.
When A is LOW, $\mathrm{Q}_{0}$ will be OFF and F will be at HIGH level.
Now it is required that the voltage at $F$ is sufficient to ensure all the load gates $Q_{1}$ to $Q_{n}$ saturated. Each load gate added to F will require a certain base current to cause saturation of the load transistor.

Note, $\quad \mathrm{I}_{\mathrm{C}(\mathrm{EOS})}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}(\mathrm{sat})}\right) / \mathrm{R}_{\mathrm{C}} \quad$ and $\quad \mathrm{I}_{\mathrm{B}(\mathrm{EOS})}=\mathrm{I}_{\mathrm{C}(\mathrm{EOS})} / \beta_{\mathrm{F}}$
Now for one load gate, the base current for the load transistor $I_{B}=\left(V_{C C}-V_{B E(s a t)}\right) /\left(R_{C}+R_{B}\right)$
For two load gate, $\mathrm{I}_{\mathrm{B} 2}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{BE}(\text { sat })}\right) /\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{B}} / 2\right)$
For total N load gate, $\mathrm{I}_{\mathrm{BT}}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{BE}(\text { sat })}\right) /\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{B}} / \mathrm{N}\right)$
For a maximum fanout of $\mathrm{N}, \mathrm{I}_{\mathrm{BT}} \geq \mathrm{N}_{\mathrm{B}(\mathrm{EOS})}$
Therefore $\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{BE}(\text { sat })}\right) /\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{B}} / \mathrm{N}\right) \geq \mathrm{N}\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}(\text { sat })}\right) /\left(\mathrm{R}_{\mathrm{C}} \beta_{\mathrm{F}}\right)$
Substituting, $\mathrm{N} \leq 50(5-0.7) /(5-0.2)-(10 / 1)=34.9 \quad$ Rounding down $\mathrm{N}=34$

## Alternate Calculation:

A limit in the fanout is set when the voltage at F is insufficient to cause the transistor of the load gate to saturate. Note that $\mathrm{V}_{\mathrm{IH}}=1.66 \mathrm{~V}$

Then $\mathrm{I}_{\mathrm{BT}}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{F}}\right) / \mathrm{R}_{\mathrm{C}}=(5-1.66) / 1=3.34 \mathrm{~mA}$
$\mathrm{I}_{\mathrm{B}}=\left(\mathrm{V}_{\mathrm{F}}-\mathrm{V}_{\mathrm{BE}(\mathrm{sat})}\right) / \mathrm{R}_{\mathrm{B}}=(1.66-0.7) / 10=0.096 \mathrm{~mA}$
$\mathrm{N}=\mathrm{I}_{\mathrm{BT}} / \mathrm{I}_{\mathrm{B}}=34.79 \rightarrow 34$

## Effect of Noise Margin on Fanout

Inclusion of Noise Margin reduces the fanout in the following manner
For a 0.5 V noise margin
Minimum HIGH level voltage at F
$\mathrm{V}_{\mathrm{OH}}=\mathrm{V}_{\mathrm{IH}}+\mathrm{NM}_{\mathrm{H}}=1.66+0.5=2.16 \mathrm{~V}$
With $\mathrm{V}_{\mathrm{F}}$ at 2.16 V there remains an in-built safety margin at the input of load gates.
Similar calculation as above gives
$\mathrm{I}_{\mathrm{BT}}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{F}}\right) / \mathrm{R}_{\mathrm{C}}=(5-2.16) / 1=2.84 \mathrm{~mA}$
$\mathrm{I}_{\mathrm{B}}=\left(\mathrm{V}_{\mathrm{F}}-\mathrm{V}_{\mathrm{BE}(\text { sat })}\right) / \mathrm{R}_{\mathrm{B}}=(2.16-0.7) / 10=0.15 \mathrm{~mA}$
$\mathrm{N}=\mathrm{I}_{\mathrm{BT} /} / \mathrm{I}_{\mathrm{B}}=19.4 \rightarrow 19$
An increased $\mathrm{NM}_{\mathrm{H}}$ reduces fanout even further.

## The Base Overdrive Factor (k)

This is the ratio of actual base current and the base current required to just saturate the transistor. This is to account for transistor parameter variation like $\beta_{\mathrm{F}}$.

For $\mathrm{V}_{\mathrm{BE}(\text { sat })}=0.7 \mathrm{~V}, \mathrm{~V}_{\mathrm{CE}(\text { sat })}=0.2 \mathrm{~V}, \beta_{\mathrm{F}}=50, \mathrm{R}_{\mathrm{C}}=1 \mathrm{~K} \Omega, \mathrm{R}_{\mathrm{B}}=10 \mathrm{~K} \Omega, 10$ load gates
$\mathrm{I}_{\mathrm{B}(\mathrm{EOS})}=\mathrm{I}_{\mathrm{C}(\mathrm{EOS})} / \beta_{\mathrm{F}}=(5-0.2) /(1 \mathrm{x} 50)=0.096 \mathrm{~mA}, \quad \mathrm{I}_{\mathrm{BT}}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{BE}(\mathrm{sat})}\right) /\left(\mathrm{R}_{\mathrm{C}}+\mathrm{R}_{\mathrm{B}} / 10\right)$
$\mathrm{I}_{\mathrm{BT}}=(5-0.7)(1+10 / 10)=2.15 \mathrm{~mA}_{\mathrm{B}} \quad \mathrm{I}_{\mathrm{B}}=\mathrm{I}_{\mathrm{BT}} / 10=0.215 \mathrm{~mA}$
Hence, $\mathrm{k}=0.215 / 0.096=2.24$

## Worst-case Design

Here, circuit is analyzed by using the particular combination of parameter values which will result in an extreme value of the desired variable.

Analysis for fanout including overdrive factor k :

$$
\mathrm{N} \leq \frac{\beta_{\mathrm{F}}}{\mathrm{k}} \cdot \frac{\mathrm{~V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{BE}(\mathrm{sat})}}{\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}(\mathrm{sat})}}-\frac{\mathrm{R}_{\mathrm{B}}}{\mathrm{R}_{\mathrm{C}}}
$$

For worst case analysis, to choose extreme values of the variables in RHS that minimizes fanout.

$$
\mathrm{N} \leq \frac{\underline{\beta}_{\mathrm{F}}}{\mathrm{k}} \cdot \frac{\underline{\mathrm{~V}}_{\mathrm{CC}}-\forall_{\mathrm{BE}(\mathrm{sat})}}{\forall_{\mathrm{CC}}-\underline{\mathrm{V}}_{\mathrm{CE}(\mathrm{sat})}}-\frac{\mathrm{R}_{\mathrm{B}}}{\underline{\mathrm{R}}_{\mathrm{C}}}
$$

Then underlined variables are to be at maximum and those have double strikethrough are to be at minimum. Since $\mathrm{V}_{\mathrm{CC}}$ falls under both we have to check both the cases. Also $\mathrm{R}_{\mathrm{B}}$ and $\mathrm{R}_{\mathrm{C}}$ generally increase or decrease together in same percentage terms.

If $\quad 4.5<\mathrm{V}_{\mathrm{CC}}<5.5, \quad 0<\mathrm{V}_{\mathrm{CE}(\text { sat) }}<0.5, \quad 20<\beta_{\mathrm{F}}<100, \quad 0<\mathrm{V}_{\mathrm{BE}(\text { sat) }}<0.5, \quad \mathrm{k}=1$
With $\mathrm{V}_{\mathrm{CC}}$ at minimum,

$$
\mathrm{N} \leq \frac{20}{1} \cdot \frac{4.5-1}{4.5-0}-\frac{10}{1} \quad \text { or } \mathrm{N} \leq 5.5
$$

With $\mathrm{V}_{\mathrm{CC}}$ at maximum,

$$
\mathrm{N} \leq \frac{20}{1} \cdot \frac{5.5-1}{5.5-0}-\frac{10}{1} \quad \text { or } \mathrm{N} \leq 6.4
$$

Therefore in worst case situation fanout is 5 .

## Resistor Transistor Logic

This was among first commercially available digital IC s introduced by Fairchild in 1961.


FIGURE 3.5
Circuit diagram of an RTL gate.

Motorola MC824AP, Quad 2 input NOR gate
$\mathrm{V}_{\mathrm{CC}}=3.6 \mathrm{~V}, \mathrm{R}_{\mathrm{B}}=450 \Omega, \mathrm{R}_{\mathrm{C}}=640 \Omega$,

$\mathrm{V}_{\text {in }}$ vs. $\mathrm{V}_{\text {out }}$ curve for MC824AP RTL gate( $\mathrm{n}=1$ and $\mathrm{n}=5$ )
Vertical scale $0.5 \mathrm{~V} /$ division, Horizontal scale $0.2 \mathrm{~V} /$ division
We see $\mathrm{V}_{\mathrm{OL}} \approx 0.15 \mathrm{~V}, \quad \mathrm{~V}_{\mathrm{IL}} \approx 0.6 \mathrm{~V}$, HIGH output is function of number of load gates.
For 5 load gates, logic swing $=\mathrm{V}_{\mathrm{OH}}-\mathrm{V}_{\mathrm{OL}}=1.15-0.15=1.0 \mathrm{~V}$

$$
\begin{aligned}
& \mathrm{NM}_{\mathrm{L}}=\mathrm{V}_{\mathrm{IL}}-\mathrm{V}_{\mathrm{OL}}=0.6-0.15=0.45 \mathrm{~V} \\
& \mathrm{NM}_{\mathrm{H}}=\mathrm{V}_{\mathrm{OH}}-\mathrm{V}_{\mathrm{IH}}=1.15-0.70=0.45 \mathrm{~V}
\end{aligned}
$$

## Power Dissipation

With all 4 inputs at HIGH level, $\mathrm{PD}_{\mathrm{H}}=4 \times 25=100 \mathrm{~mW}$
With all 4 inputs at LOW level, $\mathrm{PD}_{\mathrm{L}}=4 \times 7.5=30 \mathrm{~mW}$
Average power dissipation is calculated assuming inputs spend as much time in HIGH state as in LOW state

$$
\mathrm{PD}_{\mathrm{av}} \text { per gate }=(25+7.5) / 2=16 \mathrm{~mW}
$$

## Propagation Delay

Due to circuit capacitances and the finite switching speed of transistors, there is a delay from the time a signal is applied to the input of a logic gate until the desired change appears at the output of a gate.

$V_{\text {in }}$ on top and $V_{\text {out }}$ at bottom. Horizontal scale $10 \mathrm{~ns} /$ division

Turn on delay $=\mathrm{t}_{\mathrm{PHL}}:$ Delay in output changing from HIGH to LOW
Turn off delay $=\mathrm{t}_{\text {PLH }}:$ Delay in output changing from LOW to HIGH
Propagation delay $t_{\text {PD }}$ is average of turn on and turn off delay. Here $t_{\text {PD }} \approx 12 \mathrm{~ns}$

## Figure of Merit

It is sometimes possible to decrease the propagation delay time by increasing operating current of transistors in the circuit. But that increases power consumption. The product

$$
F=t_{\text {PD }} \times P D
$$

serves as useful figure of merit on performance of a gate. The lower it is the better. For this gate

$$
\mathrm{F}=(12 \mathrm{~ns})(16 \mathrm{~mW})=192 \mathrm{pJ}
$$

In low power RTL gate with $\mathrm{V}_{\mathrm{CC}}=3.6 \mathrm{~V}, \mathrm{R}_{\mathrm{B}}=1.5 \mathrm{~K} \Omega, \mathrm{R}_{\mathrm{C}}=3.6 \mathrm{~K} \Omega, \mathrm{t}_{\mathrm{PD}}=27 \mathrm{~ns}$ but the power dissipation with the inputs HIGH is 5 mW per gate.

## Direct-coupled Transistor Logic

One method of reducing propagation delay time is to eliminate base resistor and make a direct connection from the collector of a driving transistor to the base of load transistor.


The circuit though simple has a severe limitation like input characteristics of all the load transistors should be well matched under all conditions. Else one of them will try to take the most of the current available in the form of current-hogging. This might lead to any of other load transistors out of saturation.

The defect can be diminished by placing a resistor in series with the base. Then the base current is less dependent on $\mathrm{V}_{\mathrm{BE}}$ characteristic of the transistor. But that is typical RTL circuit.

## Diode-Transistor Logic (DTL)

The disadvantage of RTL gate is small logic swing $(\approx 1 \mathrm{~V})$ and hence lower noise margin. A simple DTL circuit is a diode AND gate followed by an inverter giving NAND output.


FIGURE 3.12
Voltage transfer characteristic of DTL gate.
LOW level output is represented by $\mathrm{V}_{\mathrm{CE}(\text { sat) })}$. At the LOW level threshold the input voltage must be sufficiently positive to turn off the input diodes and start turning on the output transistor.
$\mathrm{V}_{\mathrm{IL}}=\mathrm{V}_{\mathrm{BE}(\text { sat })}+\mathrm{V}_{\mathrm{D} 2 \text { (on) }}-\mathrm{V}_{\mathrm{D} 1 \text { (on) }}=\mathrm{V}_{\mathrm{BE}(\text { sat) })}=0.7 \mathrm{~V}$ and $\mathrm{NM}_{\mathrm{L}}=\mathrm{V}_{\mathrm{IL}}-\mathrm{V}_{\mathrm{OL}}=0.7-0.2=0.5 \mathrm{~V}$
LOW level noise margin can be increased by placing two diodes in series instead of $\mathrm{D}_{2}$. Then
$\mathrm{V}_{\mathrm{IL}}=\mathrm{V}_{\mathrm{BE}(\text { sat })}+2 \mathrm{~V}_{\mathrm{D} 2(\text { on })}-\mathrm{V}_{\mathrm{D} 1 \text { (on) }}=\mathrm{V}_{\mathrm{BE}(\text { sat) })}+\mathrm{V}_{\mathrm{D} 2 \text { (on) }}=0.7+0.7=1.4 \mathrm{~V}$
and $\mathrm{NM}_{\mathrm{L}}=\mathrm{V}_{\mathrm{IL}}-\mathrm{V}_{\mathrm{OL}}=1.4-0.2=1.2 \mathrm{~V}$

HIGH level output is represented by $\mathrm{V}_{\mathrm{CC}}\left(=\mathrm{V}_{\mathrm{OH}}\right)$. Then input diodes of load gates are reverse biased and draws negligible reverse current. And there is no current hogging problem. The base current to transistor of a particular stage is decided by its own base resistance $\left(R_{1}\right)$.
$\mathrm{NM}_{\mathrm{H}}=\mathrm{V}_{\mathrm{OH}}-\mathrm{V}_{\mathrm{IH}}=4.0-0.9=3.1 \mathrm{~V}$
Logic swing $=\mathrm{V}_{\mathrm{OH}}-\mathrm{V}_{\mathrm{OL}}=4-0.2=3.8 \mathrm{~V}$
Transition width $=\mathrm{V}_{\mathrm{IH}}-\mathrm{V}_{\mathrm{IL}}=0.9-0.7=0.2 \mathrm{~V}$
The output of RTL acts like current source while for DTL it acts like current sink.

## Fanout of Basic DTL gate

A basic DTL circuit with two voltage offset diodes is shown.


The basic DTL gate (whose output is at the collector of $Q_{14}$ ) loaded with n
other gate inputs.
From the figure, fanout $=\left(\left(I_{C}-I_{R 3 A}\right) / I_{D}\right.$.
For $\mathrm{V}_{\mathrm{BE}(\text { sat })}=\mathrm{V}_{\mathrm{D}(\text { on })}=0.7 \mathrm{~V}, \beta_{\mathrm{F}}=20, \mathrm{~V}_{\mathrm{CE}(\text { sat })}=0.2 \mathrm{~V}, \mathrm{k}=1$
$\mathrm{I}_{\mathrm{R} 1 \mathrm{~A}}=\left(\mathrm{V}_{\mathrm{CC}}-2 \mathrm{~V}_{\mathrm{D}(\text { on })}-\mathrm{V}_{\mathrm{BE}(\text { on })}\right) / \mathrm{R}_{1 \mathrm{~A}}=(4-1.4-0.7) / 2=0.95 \mathrm{~mA}$
$\mathrm{I}_{\mathrm{R} 2 \mathrm{~A}}=\left(\mathrm{V}_{\mathrm{BE}(\text { on })}-\mathrm{V}_{\mathrm{BB}}\right) / \mathrm{R}_{2 \mathrm{~A}}=(0.7+2) / 5=0.54 \mathrm{~mA} \quad \mathrm{I}_{\mathrm{B} 1 \mathrm{~A}}=0.95-0.54=0.41 \mathrm{~mA}$
The collector current at the edge of saturation $\mathrm{I}_{\mathrm{C}}=20 \mathrm{x} 0.41=8.2 \mathrm{~mA}$
$\mathrm{I}_{\mathrm{R} 3 \mathrm{~A}}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}(\mathrm{sat})}\right) / \mathrm{R}_{3 \mathrm{~A}}=(4-0.2) / 4=0.95 \mathrm{~mA}$

At the output gate transistor base
$\mathrm{V}_{\mathrm{B} 1}=\mathrm{V}_{\mathrm{CE}(\text { sat })}+\mathrm{V}_{\mathrm{D}(\text { on })}-2 \mathrm{~V}_{\mathrm{D} \text { (on) }}=\mathrm{V}_{\mathrm{CE}(\text { sat })}-\mathrm{V}_{\mathrm{D} \text { (on) }}=0.2-0.7=-0.5 \mathrm{~V}$
These transistors are cut off.
$\mathrm{I}_{\mathrm{R} 1 \mathrm{~B}}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}(\text { sat })}-\mathrm{V}_{\mathrm{D}(\text { on })}\right) / \mathrm{R}_{1 \mathrm{~B}}=(4-0.2-0.7) / 2=1.55 \mathrm{~mA}$
$\mathrm{I}_{\mathrm{R} 2 \mathrm{~B}}=\left(\mathrm{V}_{\mathrm{B} 1}-\mathrm{V}_{\mathrm{BB}}\right) / \mathrm{R}_{2 \mathrm{~B}}=(-0.5+2) / 5=0.3 \mathrm{~mA} \quad \mathrm{I}_{\mathrm{D}}=1.55-0.3=1.25 \mathrm{~mA}$
Then, fanout $\mathrm{N}=(8.2-0.95) / 1.25=5.8 \rightarrow 5$
Note that this is not worst case fanout.

## Modified DTL Gate



The first circuit shows removal one level shifting diode by one emitter follower. This increases base current to $\mathrm{Q}_{2}$ increasing fanout.. $\mathrm{R}_{4}$ prevents $\mathrm{Q}_{2}$ going deep in saturation if less load is connected. But then $\mathrm{Q}_{1}$ also saturates.

The feedback biasing second circuit (through $\mathrm{R}_{1}$ ) prevents $\mathrm{Q}_{1}$ from saturating. As collector current increases, collector voltage falls and base current too falls.

## Fanout calculation

$\mathrm{V}_{\mathrm{CC}}-3 \mathrm{~V}_{\mathrm{BE}(\text { on })}=\mathrm{I}_{\mathrm{B} 1}\left(\mathrm{R}_{1}+\mathrm{R}_{4}\right)+\mathrm{I}_{\mathrm{C} 1} \mathrm{R}_{4} \quad$ and $\quad \mathrm{I}_{\mathrm{C} 1}=\beta_{\mathrm{F}} \mathrm{I}_{\mathrm{B} 1} \quad$ since $\mathrm{Q}_{1}$ is not saturated.
Base current of $\mathrm{Q}_{1}: \mathrm{I}_{\mathrm{B} 1}=\frac{\mathrm{V}_{\mathrm{CC}}-3 \mathrm{~V}_{\mathrm{BE}(\text { on })}}{\left(\mathrm{R}_{1}+\mathrm{R}_{4}\right)+\beta_{\mathrm{F}} \mathrm{R}_{4}}=(5-2.1) /(3.75+20 \times 1.75)=0.075 \mathrm{~mA}$
$\mathrm{I}_{\mathrm{C} 1}=\beta_{\mathrm{F}} \mathrm{I}_{\mathrm{B} 1}=20 \mathrm{x} 0.075=1.5 \mathrm{~mA}$
Note, $\mathrm{V}_{\mathrm{C} 1}=\mathrm{V}_{\mathrm{CC}}-\mathrm{R}_{4}\left(\mathrm{I}_{\mathrm{C}}+\mathrm{I}_{\mathrm{B}}\right)=5-1.75 \times 1.575=2.25 \mathrm{~V}, \quad \mathrm{~V}_{\mathrm{B} 1}=2.1 \mathrm{~V}$. So BC is reverse biased and hence in active region.

Now $\mathrm{I}_{\mathrm{E} 1}=0.075+1.5=1.58 \mathrm{~mA} \quad$ and $\quad \mathrm{I}_{\mathrm{B} 2}=\mathrm{I}_{\mathrm{E} 1}-\mathrm{V}_{\mathrm{B} 2} / \mathrm{R}_{2}=1.58-0.7 / 5=1.44 \mathrm{~mA}$
The collector current of $\mathrm{Q}_{2}$ at the edge of saturation $\mathrm{I}_{\mathrm{C} 2}=\beta_{\mathrm{F}} \mathrm{I}_{\mathrm{B} 2}=20 \mathrm{x} 1.44=28.8 \mathrm{~mA}$
$\mathrm{I}_{\mathrm{R} 3}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}(\mathrm{sat})}\right) / \mathrm{R}_{3}=(5-0.2) / 6=0.8 \mathrm{~mA}$

For the load gates input is LOW
So $\mathrm{V}_{\mathrm{B} 1(\mathrm{~L})}=\mathrm{V}_{\mathrm{CE}(\text { sat })}+\mathrm{V}_{\mathrm{D}(\text { on })}=0.2+0.7=0.9 \mathrm{~V}$
This voltage is insufficient to turn on $\mathrm{Q}_{1}$ thorough $\mathrm{D}_{2}$.
Then $\mathrm{I}_{\mathrm{D}}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}(\text { sat })}-\mathrm{V}_{\mathrm{D}(\text { on })}\right) /\left(\mathrm{R}_{1}+\mathrm{R}_{4}\right)=(5-0.2-0.7) / 3.75=1.09 \mathrm{~mA}$
Then, fanout $\mathrm{N}=(28.8-0.8) / 1.09=25.6 \rightarrow 25$
Note, in high threshold DTL, $\mathrm{D}_{2}$ is replaced with zener diode of $6 \mathrm{~V}, \mathrm{~V}_{\mathrm{CC}}$ is 15 V and to avoid excessive power dissipation the values of resistors are increased.

MC930 dual expandable 4 input gate with following specification:
$\mathrm{V}_{\mathrm{OH}}=2.6 \mathrm{~V}, \mathrm{~V}_{\mathrm{OL}}=0.4 \mathrm{~V}, \mathrm{~V}_{\mathrm{IL}}=1.1 \mathrm{~V}, \mathrm{~V}_{\mathrm{IH}}=2.0 \mathrm{~V}, \mathrm{P}_{\mathrm{DH}}=11.9 \mathrm{~mW}, \mathrm{P}_{\mathrm{DL}}=5.45 \mathrm{~mW}, \mathrm{~F}=285 \mathrm{pJ}$
RTL thus is faster. But fanout, logic swing, noise margin are greater.

## Transistor-Transistor Logic (TTL)

The fact that the characteristics of BE junction of a transistor is similar to a diode is used to advantage in TTL logic circuit. The input diodes of a DTL gate are replaced by a multi emitter transistor. The CB junction provides an offset voltage like an offset diode. The advantages are: (1) Silicon area saved (2) Improvement of switching speed (turning off of $\mathrm{Q}_{3}$ ).


With input LOW $\left(V_{C E(s a t)}\right)$ :
$B E$ junction of $Q_{1}$ is forward biased. But $I_{C}$ for $Q_{1}$ is only leakage current of $D_{2}$ which is very small ( $\ll \beta_{\mathrm{F}} \mathrm{I}_{\mathrm{B}}$ ) and hence $\mathrm{Q}_{1}$ is in saturation. So voltage at collector of $\mathrm{Q}_{1}$ is nearly 0.2 V higher than the emitter voltage. So insufficient voltage to forward bias $D_{2}$ and subsequently $Q_{3}$. $\mathrm{Q}_{3}$ is off. Output is held at $\mathrm{V}_{\mathrm{CC}}$, HIGH logic level.

## With all inputs at $\mathrm{HIGH}\left(V_{C C}\right)$ :

$B E$ junction of $Q_{1}$ is reverse biased. Current flows from $V_{C C}$ through $R_{1}$, forward biased $B C$ junction of $Q_{1}, D_{2}$ into $B E$ junction of $Q_{3}$. This current is sufficient to saturate $Q_{3}$ resulting LOW logic level at the output of the gate.

Note that the input transistor now works in the inverse mode with E and C changing their roles. With emitter acting as collector
$\mathrm{I}_{\mathrm{E} 1}=\beta_{\mathrm{R}} \mathrm{I}_{\mathrm{B} 1}=\beta_{\mathrm{R}} \mathrm{I}_{\mathrm{B}} / \mathrm{M}$ where $\mathrm{M}=$ Total no. of emitters in $\mathrm{Q}_{1}$ and $\mathrm{I}_{\mathrm{B}}=$ Total base current
$\mathrm{I}_{\mathrm{C} 1}=\left(\beta_{\mathrm{R}}+1\right) \mathrm{I}_{\mathrm{B} 1}+\left(\beta_{\mathrm{R}}+1\right) \mathrm{I}_{\mathrm{B} 2}+\ldots=\left(\beta_{\mathrm{R}}+1\right) \mathrm{I}_{\mathrm{B}}$

(a) When inputs $A$ and $B$ are both $0 \mathrm{~V}, Q_{A}$ and $Q_{B}$ are both ON , so $Q_{2}$ is OFF.

(b) When input $A$ (or input $B$ ) is $0 \mathrm{~V}, Q_{A}$ (or $Q_{B}$ ) is on, so $Q_{2}$ is off.

(c) When inputs $A$ and $B$ are both $+5 \mathrm{~V}, Q_{A}$ and $Q_{B}$ are both OFF. Current flows from base to collector in $Q_{A}$ and $Q_{B}$, supplying base current to turn on $Q_{2}$.

## Modification

The previous circuit gives problem if $\beta_{\mathrm{R}}$ is high, then a large amount of current flows to input. This current with collector load resistance can bring down HIGH level voltage considerably. A totem-pole output reduces output resistance for both HIGH \& LOW output.


Note that for all logic families like RTL, DTL, modified DTL for LOW level output resistance is nearly 10 ohm while for HIGH level it is 650-6000 ohm. With totem-pole TTL gives output resistance of less than 100 ohm for HIGH level output. This also quickens charging/discharging of capacitance at the gate output.
$\mathrm{Q}_{2}$ besides serving as level shifter similar to $\mathrm{D}_{2}$ acts as phase splitter. Voltage at $\mathrm{C} \& \mathrm{E}$ of $\mathrm{Q}_{2}$ are 180 degree out of phase. Thus when there is LOW at E of $\mathrm{Q}_{2}$ to turn off $\mathrm{Q}_{3}$ there is HIGH at C of $\mathrm{Q}_{2}$ to turn on $\mathrm{Q}_{4}$ and vice versa.

The diode $\mathrm{D}_{1}$ is required to avoid an indeterminate output level. With LOW level at output both $\mathrm{Q}_{2}$ and $\mathrm{Q}_{3}$ are saturated. Their collector voltages w.r.t. ground are 0.9 V and 0.2 V respectively. The voltage 0.9 V in absence of $\mathrm{D}_{1}$ turns on $\mathrm{Q}_{4}$. Then current will be diverted from collector of $\mathrm{Q}_{2}$ to base of $\mathrm{Q}_{4}$ and thus $\mathrm{Q}_{2}$ will come out of saturation. Then both $\mathrm{Q}_{3}$ and $\mathrm{Q}_{4}$ will be conducting resulting in indeterminate output level.


Figure 10.4
Static analysis of one gate in a 7400 quad 2-input NaND gate, including the totem pole output.

Why not $R_{3}=0$ ?
With input HIGH, $\mathrm{Q}_{3}$ in saturation and output LOW.
Now input going LOW, $\mathrm{Q}_{2}$ turns off, its collector rises turning on $\mathrm{Q}_{3}$. If $\mathrm{Q}_{3}$ is slow to come out of saturation both the transistors are on briefly and high current may result. During this switching

$$
\mathrm{I}=\left(\mathrm{V}_{\mathrm{CC}}-\left(\mathrm{V}_{\mathrm{CE} 3 \text { (sat) }}+\mathrm{V}_{\mathrm{Dl} \text { (on) }}+\mathrm{V}_{\mathrm{CE} 4(\text { sat) })}\right)\right) / \mathrm{R}_{3}=30 \mathrm{~mA} \text { (comes as spike in power supply) }
$$

Note this also protects when logic HIGH output is accidentally grounded to limit the current.

## Fanout of TTL Gate

With output LOW:

## Figure 10.7

A TTL output driving several TTL loads. $I_{\mathrm{OL}}$ is the sum of the currents supplied by the loads and $Q_{4}$ must be capable of sinking all of this current.


To consider how much current $\mathrm{Q}_{3} \underline{\text { can sink first. Note that } \mathrm{Q}_{2} \text { and } \mathrm{Q}_{3} \text { both are in saturation. }}$
Now at $\mathrm{Q}_{1}, \quad \mathrm{~V}_{\mathrm{B} 1}=2 \mathrm{~V}_{\mathrm{BE}(\text { sat })}+\mathrm{V}_{\mathrm{BC}(\text { sat })}=2 \mathrm{x} 0.7+0.5=1.9 \mathrm{~V}$

$$
\left[\mathrm{V}_{\mathrm{BC}(\mathrm{sat})}=0.5 \mathrm{~V}\right]
$$

Then $\mathrm{I}_{\mathrm{B} 1}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{B} 1}\right) / \mathrm{R}_{1}=(5-1.9) / 4=0.78 \mathrm{~mA}$
Then $\mathrm{I}_{\mathrm{C} 2}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}(\text { sat })}-\mathrm{V}_{\mathrm{BE}(\text { sat) })}\right) / \mathrm{R}_{4}=(5-0.2-0.7) / 1.6=2.56 \mathrm{~mA}$
Note that, $\mathrm{I}_{\mathrm{B} 2}=\mathrm{I}_{\mathrm{C} 1}=\left(\beta_{\mathrm{R}}+1\right) \mathrm{I}_{\mathrm{B} 2}$
If $\beta_{\mathrm{R}}=0.2$ then $\beta_{\mathrm{F}}=\mathrm{I}_{\mathrm{C} 2} /\left[\left(\beta_{\mathrm{R}}+1\right) \mathrm{I}_{\mathrm{B} 2}\right]=2.56 /(1.2 \times 0.78)=2.8$ is sufficient to saturate $\mathrm{Q}_{2}$.
Again, $\mathrm{I}_{\mathrm{B} 3}=\mathrm{I}_{\mathrm{B} 2}+\mathrm{I}_{\mathrm{C} 2}-\mathrm{V}_{\mathrm{BE}(\text { sat })} / \mathrm{R}_{2}=0.93+2.56-0.6 / 1=2.79 \mathrm{~mA}$
At the EOS for $\mathrm{Q}_{3}, \quad \mathrm{I}_{\mathrm{C} 3}=\beta_{\mathrm{F}} \mathrm{I}_{\mathrm{B} 3}=20 \mathrm{x} 2.79=55.8 \mathrm{~mA} \quad\left(\right.$ Typical value of $\left.\beta_{\mathrm{F}}=20-100\right)$

To consider how much is the load current next.
$\mathrm{I}_{\mathrm{E} 1}=\left(\mathrm{V}_{\mathrm{CC}}-\mathrm{V}_{\mathrm{CE}(\text { sat })}-\mathrm{V}_{\mathrm{BE}(\text { sat) })}\right) / \mathrm{R}_{1}=(5-0.2-0.7) / 4=1.02 \mathrm{~mA} \quad$ [Since, $\beta_{\mathrm{R}}$ is small.]
So $\mathrm{N}_{\mathrm{L}}=\mathrm{I}_{\mathrm{C} 3} / \mathrm{I}_{\mathrm{E}}=55.8 / 1.02 \rightarrow 54$

## With output HIGH :

Let us calculate the fanout possible if output HIGH voltage level becomes 2.4 V due to loading effect.

With $\mathrm{Q}_{4}$ conducting, voltage at base of $\mathrm{Q}_{4}=2 \times 0.7+2.4=3.8 \mathrm{~V}$
Then $Q_{2}$ is cut off and voltage drop across $R_{4}$ is due to base current of $Q_{4}$.
$\mathrm{I}_{\mathrm{B} 4}=(5-3.8) / 1.6=0.75 \mathrm{~mA} \quad$ and $\quad \mathrm{I}_{\mathrm{C} 4}=(5-0.2-0.7-2.4) / 0.13=13.1 \mathrm{~mA}$
$\mathrm{I}_{\mathrm{E} 4}=\mathrm{I}_{\mathrm{B} 4}+\mathrm{I}_{\mathrm{C} 4}=13.85 \mathrm{~mA}$
The base current of the load transistor $\mathrm{Q}_{1}$ is determined as 0.78 mA . It acts in inverse mode. With $\beta_{\mathrm{R}}=0.2$ input current to load gate $=0.2 \times 0.78=0.156 \mathrm{~mA}$

Then $\mathrm{N}_{\mathrm{H}}=13.8 / 0.156 \rightarrow 88$ ( $=176$ if two emitter)
[Note, $\mathrm{N}_{\mathrm{H}}>\mathrm{N}_{\mathrm{L}}$ is common to TTL gate circuits.]

## 54 series TTL

Recommended $\mathrm{V}_{\mathrm{CC}}=5.0 \mathrm{~V} \pm 10$ percent ; Operating Temperature -55 to +125 degree centigrade
Fanout $=10, \mathrm{~V}_{\mathrm{OH}}=3.1 \mathrm{~V}, \mathrm{~V}_{\mathrm{OL}}=0.2 \mathrm{~V}, \mathrm{~V}_{\mathrm{IL}}=1.2 \mathrm{~V}, \mathrm{~V}_{\mathrm{IH}}=1.4 \mathrm{~V}$
Short circuit output current $=34 \mathrm{~mA}$
[ $\mathrm{I}_{\mathrm{C} 4(\text { sat })}$ with output at $0 \mathrm{~V}=(5-0.2-0.7-0) / 0.13=31.6 \mathrm{~mA} \quad$ and $\left.\quad \mathrm{I}_{\mathrm{B} 4}=(5-1.4) / 1.6=2.2 \mathrm{~mA}\right]$
$\mathrm{V}_{\mathrm{CC}}$ supply current per gate when output LOW, no load(sum of $\mathrm{I}_{\mathrm{C} 2}$ and $\left.\mathrm{I}_{\mathrm{B} 2}\right)=3.6 \mathrm{~mA}$
$\mathrm{V}_{\mathrm{CC}}$ supply current per gate when output HIGH, no load $\left(\mathrm{I}_{\mathrm{B} 1}=\mathrm{I}_{\mathrm{E} 1}\right)=1.1 \mathrm{~mA}$
Power dissipation $=\mathrm{V}_{\mathrm{CC}}\left(\mathrm{I}_{\mathrm{CCL}}+\mathrm{I}_{\mathrm{CCH}}\right) / 2=10 \mathrm{~mW}$
Typical propagation delay, $\mathrm{t}_{\mathrm{pd}}=9 \mathrm{~ns} \quad$ Figure of merit $=9 \mathrm{x} 10=90 \mathrm{pJ}$


## High Speed (H) and Low Power (L) TTL

In High Speed TTL, lower resistance values are used with an additional pull up transistor $\mathrm{Q}_{5}$ in the form of Darlington pair which has much greater current gain. The diode in the totempole output no longer needed.

(a) 74H00 NAND gate.

(b) 74L00 NAND gate.

Figure 10.8
Typical high-speed $(H)$ and low-power $(L)$ TTL gates.

For low power TTL, larger resistance values are used, which reduces power consumption at the expense of speed.

## Schottky (S) and Low Power Schottky (LS) TTL

This is to prevent transistor going deep into saturation by clamping BC forward bias voltage. This reduces storage time delay as excess charge carriers are prevented at the junction. A clamp of less than 0.7 V is required. Though Ge diode can provide that but it is difficult to fabricate it on Si chips. Schottky diode having metal-semiconductor junction with forward drop of 0.3-0.4V is used.

(a) Schottky diode construction.

(c) A Schottky-clamped NPN transistor.

(b) Schottky diode symbol.

(d) Equivalent symbol for (c).

Figure 10.9
The Schottky diode and Schottky clamp.

(a) One gate in the 74 S 00 quad two-input Nand gate.

## Advanced Schottky (AS) and Advanced Low Power Schottky (ALS) TTL

ALS and AS technologies are recent enhancements in the form of doping technique (ion implantation instead of diffusion), improved isolation (reduces capacitance and improves switching time), and addition of more complex circuitry to have higher speed, lower power consumption and increased fanout.

(a) One gate in the 74ALSO0A quad 2-input NAND gate.

(b) Equivalent input switching circuit.

Figure 10.13
Typical advanced Schottky (AS) and advanced low-power Schottky (ALS) gates.


Figure 10.12
Comparison of fanouts for TTL subfamilies.

## Open-Collector outputs - Wired AND

The output of such gates are simply the collector of the pull-down transistor, which the user may connect to an external resistor and power-supply voltage. LED, relay coils can be connected at the output also it can be used to logically AND the outputs of the gates. The resistance is also called pull up resistor.


(b) Switching equivalent of (a). The output is high only if $Q_{1}$ and $Q_{2}$ are both open; i.e., only if the outputs of gates 1 and 2 are both high.

(c) Wire-Anded output of two nand gates.

(d) The wire-anded output of inverters implements the NOR operation.

Absence of pull up transistor reduces switching speed. However the are useful in reducing chip count of a system where speed is not a consideration.

## Three (Tri) State Logic

Tristae Logic is used to prevent HIGH output being short circuited with LOW output e.g. for bus drivers in sharing a bus.

(b) Input device 1 is effectively disconnected from the bus while input device 2 is connected to it. The open switches represent high-impedance states. When its $E$ (enable) input is high, a device has control of the bus.

This has an addition Control input in the form of ENABLE. The circuit operates normally when enabled. Else the output goes into a high impedance state (third state) where it neither drives nor sinks current. IC 74AS231 is TTL 8 input bus driver.


Figure 10.18
An example of a TTL inverter modified for three-state operation. The output is high impedance when $\overline{E N A B L E}$ is high, the case illustrated here.


[^0]:    Dr. Goutam Saha
    Assistant Professor
    Dept. of Electronics \& Electrical Communication Enginnering
    Indian Institute of technology
    Kharagpur INDIA 721302
    Tel: 91-3222-83556 (O), 91-3222-83557 (R)
    email: saha_goutam@hotmail.com, gsaha@ece.iitkgp.ernet.in

